In situ study on the compression deformation of MoNbTaVW high-entropy alloy

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\textbf{A B S T R A C T}

The excellent mechanical properties of high-entropy alloys (HEAs) make them promising materials for advances in science and technology. However, the underlying mechanism of plastic deformation is not well understood. In situ experiments are urgently required to provide a fundamental understanding of the plastic deformation under high pressure. We performed in situ synchrotron X-ray diffraction (XRD) experiments to study compression deformation behavior of the HEA MoNbTaVW in a radial diamond anvil cell (rDAC). Our results show that the strength and ratio of the stress-to-shear modulus values are ~1.5 and 3 times that of pure tungsten (W), respectively. MoNbTaVW showed plastic deformation above 5 GPa and displayed a much stronger texture. We found that the active dislocation behavior is mainly responsible for the high strength in MoNbTaVW under compression. This unique technique opens a new avenue to investigate the in situ mechanical properties and their mechanism in other types of HEAs.

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1. Introduction

Compared with pure metals, high-entropy alloys (HEAs) have demonstrated many promising properties [1–4], such as high strength at both room temperature and high temperature [5], exceptional ductility and toughness [6], and they are considered as a new class of advanced structural materials. The studies on refractory HEAs were inspired by their wide range of fundamental properties, which provide the high flexibility of refractory HEAs. As one typical example of a refractory HEA, the body-centered cubic (BCC) MoNbTaVW has shown high hardness and exceptional strength at temperatures up to 1900 K [7,8]. Coarse-grained MoNbTaVW showed a high Vickers micro-hardness of 5250 MPa [9], while nanocrystalline MoNbTaVW, with an average particle size of ~30 nm, had a high hardness of 11.4 GPa at 1150 °C [8]. On the other hand, the yield stress of MoNbTaVW with grain size of ~80 µm was measured using standard compression techniques (Instron mechanical testing machine). It is 1246 MPa at room temperature and only decreases to 842 MPa at 1000 °C [7]. The yield stress has been shown to be extremely sensitive to the length scale of the microstructure, which depends on synthesis conditions. Maresca and Curtin [10] presented a theory of edge-dislocation strengthening in BCC random alloys to rationalize the strength of MoNbTaVW and other BCC HEAs. Since the random field of solutes in these high-concentration alloys creates large energy barriers for thermally activated edge glide, the strength of BCC HEAs can be controlled by edge dislocations, especially at high temperatures.

In the past several years, many experimental efforts have also been made on understanding the mechanism responsible for the HEAs outstanding mechanical properties [11–13], which is crucial for material design and realistic application of high performance HEAs.

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Traditional mechanical testing, whether tensile or compressive experiments, typically utilize ex situ methods to characterize the microstructure. Common examples include, the investigation of grain size and deformation texture by scanning electron microscopy (SEM) and electron backscatter diffraction (EBSD) [14], element distribution by energy dispersive spectroscopy (EDS) [15], and plastic deformation and defect (such as twinning, dislocation) behavior by transmission electron microscopy (TEM) [4,16,17]. Compression techniques have also been used to investigate deformation mechanical behavior and its mechanism by studying the samples ex situ after compression [18]. There are some tentative works that incorporate TEM with tension stage, which allows one to monitor the dislocation formation and movement in situ [15]. Nevertheless, in situ investigations, as a function of temperature and pressure, are still urgently required, if the active deformation mechanisms in HEAs are to be fully understood.

A diamond anvil cell (DAC) [19], which can easily generate high pressure by compressing small samples between two opposing diamond culets, is widely used in material science to explore significant changes in the properties of materials induced by high pressure. Previously, DAC-based high-pressure techniques, especially high-pressure X-ray diffraction (XRD), have been used to investigate the phase transition of several 3D transition metal HEAs, such as CoCrFeMnNi, AlCoCrFeNi, and CoCrCuFeNi at the micrometer scale [20–25]. Compared with conventional axial XRD, the technique of radial XRD in a radial DAC (rDAC) makes it possible to investigate the texture and lattice strain in stressed crystals in situ. For example, in situ observation of plastic deformation and active grain rotation in nanometer-scaled Ni were reported by applying the rDAC XRD technique [26,27]. A similar technique was also used to reveal the martensitic transition mechanism in oxides under high pressure [28,29]. For superhard materials, the rDAC technique has become a powerful in situ tool to study their elastic and plastic mechanical properties, such as bulk modulus, shear stress, and yield stress [30,31]. Most importantly, the data collected from the rDAC XRD method have a much better statistical reliability because of the large sample volume (μm³ scale), compared with a local study done by TEM (nm² scale). Therefore, the rDAC XRD technique is a powerful in situ characterization method to study the deformation behavior of materials, including HEAs.

In this work, the rDAC XRD experiments were carried out in situ to study the deformation behavior of the HEA MoNbTaVW. The same study on pure W was also performed as a reference to illustrate the advanced properties of HEAs. The first principles density functional theory (DFT) based simulations were employed as an accessorial tool to help understand the mechanism of the mechanical properties under high pressure. Our study shows that MoNbTaVW displayed much higher strength and stronger texture than those of pure W. This work clearly demonstrated that the active dislocation behavior is mainly responsible for the high-strength properties observed in MoNbTaVW under compression. The unique technique used in this work can be applied to study the mechanical properties and their mechanism in other types of HEAs.

2. Experiments and computational methods

The MoNbTaVW sample was prepared by arc melting on a water-cooled copper hearth under an argon atmosphere. The powders used in synthesizing the alloy with purity higher than 99.9% were mixed with equal atomic ratios and pressed to a cylindrical shape. After melting, the compounds were inverted and re-melted several times to ensure chemical homogeneity. The MoNbTaVW sample was then cut into small pieces and milled under normal temperature and pressure in the air to powder for the in situ high-pressure synchrotron XRD experiment. The average size of samples particles was 0.05–0.1 μm checked by SEM. The rDAC technique was employed to demonstrate the deformation behavior and texturing of stressed MoNbTaV/W/Au and W/Au mixtures, in which Au was used as the pressure calibrant. As shown in Fig. 1(a), a Kapton supported boron gasket, which is X-ray transparent, was clamped by the opposing diamond culets. The samples were loaded into the center hole of the boron gasket, where the diameter of the gasket hole was 60 μm. The pressure was generated by evenly applying force to the opposing diamonds. In situ rDAC XRD data were collected at beamline 12.2.2 at the Advanced Light Source (ALS), Lawrence Berkeley National Laboratory (LBNL) with the X-ray wavelength of 0.4133 Å. CeO₂ was used as the standard material to calibrate the sample-detector distance and orientation. The diffraction images were initially analyzed by Diopas [32] to determine the pressure by fitting to the standard Au diffraction peaks. The measured 2D diffraction of both samples under ambient conditions, high pressure (~20 GPa), and back to ~1 GPa are shown in Fig. 1(b) and (c), in which the complete 1 1 0, 20 0, 2 1 1 and 220 peaks as a function of pressure are shown in Fig. 2(a) and decompression are shown in Fig. 2(a) and (b), respectively. The corresponding pressures which were determined by the standard Au XRD peaks are listed on the right side of each figure. As shown in the figures, all major peaks obtained under various pressure were characterized as FCC (the standard Au diffraction peaks) and BCC (MoNbTaVW). Furthermore, the lattice constant of MoNbTaVW at ambient conditions (black XRD pattern at the bottom of Fig. 2(a)) is 0.3195 nm (DFT calculation: 0.3194 nm), while the lattice constant of pure W is 0.3164 nm (DFT: 0.3164 nm). Since neither peak appear nor disappears, there was no phase transition obtained during compression with the pressure up to 20 GPa. It is also clearly shown that all diffraction peaks shift to larger 2θ angles with pressure and shift to smaller 2θ angles when the pressure is decreased. The corresponding 2θ angles for the 110, 200, 211 and 220 peaks as a function of pressure are shown in Fig. 2(c). The location of the diffraction peaks of MoNbTaVW show a

In situ XRD patterns of the MoNbTaV/W/Au and W/Au mixtures during compression and decompression are shown in Fig. 2(a) and (b), respectively. The corresponding pressures which were determined by the standard Au XRD peaks are listed on the right side of each figure. As shown in the figures, all major peaks obtained under various pressure were characterized as FCC (the standard Au diffraction peaks) and BCC (MoNbTaVW). Furthermore, the lattice constant of MoNbTaVW at ambient conditions (black XRD pattern at the bottom of Fig. 2(a)) is 0.3195 nm (DFT calculation: 0.3194 nm), while the lattice constant of pure W is 0.3164 nm (DFT: 0.3164 nm). Since neither peak appear nor disappears, there was no phase transition obtained during compression with the pressure up to 20 GPa. It is also clearly shown that all diffraction peaks shift to larger 2θ angles with pressure and shift to smaller 2θ angles when the pressure is decreased. The corresponding 2θ angles for the 110, 200, 211 and 220 peaks as a function of pressure are shown in Fig. 2(c). The location of the diffraction peaks of MoNbTaVW show a...
greater angular dependence on applied pressure, which indicates MoNbTaW shows a greater change in lattice constant. Moreover, due to the existence of multiple elements in the alloy, different intrinsic physical properties of these elements (for example, atom size, electronegativity, covalence electrons, and so on) may induce more local stress and defects in the BCC MoNbTaW crystal, which lead to broader peaks than those of W. Consequently, the full width at half maximum (FWHM) of the MoNbTaW diffraction peaks are also broader than those of pure W.

Based on the XRD patterns under various pressures, the volume per atom as a function of pressure for MoNbTaW (red dots) and W (black dots) are demonstrated in Fig. 3(a). The corresponding lattice constants under various pressure are shown in Fig. 3(b) by the solid squares/circles. The inset of Fig. 3(b) shows a typical 125-atom SQS model. No obvious volume collapse was obtained under high pressure, indicating a stable phase of MoNbTaW and W up to ~20 GPa. The volume–pressure curves in Fig. 3(a) were fitted by the third order Birch–Murnaghan isothermal equation of state (BM3-EOS) [44,45],

$$P = 1.5B_0 \left( \frac{V_0}{V} \right)^{7/3} - \left( \frac{V_0}{V} \right)^{5/3} \left( 1 + 0.75(B_1 - 4) \left( \frac{V_0}{V} \right)^{2/3} - 1 \right)$$

where $P$ is pressure, $V_0$ is the equilibrium volume, $V$ is the deformed volume, $B_0$ is the bulk modulus, and $B_1$ is the derivative of the bulk modulus with respect to pressure. The bulk modulus of MoNbTaW obtained by fitting the BM3-EOS to the P–V curve (red dash line in
Fig. 3(a)) is 20.17 ± 5.8 GPa, with a pressure derivative of 4 and an equilibrium volume of 16.307 Å\(^3\)/atom. The bulk modulus of W (black dash line in Fig. 3(a)) is 307.7 ± 4.1 GPa with a pressure derivative of 4 and an equilibrium volume of 15.810 Å\(^3\)/atom. The small bulk modulus of MoNbTaVW represents its higher compressibility, and consequently, the shift of the XRD peaks for MoNbTaVW is more obvious than those for W with the increase of pressure, as shown in Fig. 2.

The bulk moduli of MoNbTaVW and W were also estimated by fitting the data to the Voigt–Reuss–Hill averaging scheme [46] based on DFT,

\[
B = \frac{1}{3}(C_{11} + 2C_{12}), \quad G = \frac{1}{2}(G_{\text{Voight}} + G_{\text{Reuss}})
\]

(2)

\[
G_{\text{Voight}} = \frac{1}{3}(C_{11} - C_{12} + 3C_{44}), \quad G_{\text{Reuss}} = \frac{5}{4(S_{11} - S_{12}) + 3S_{44}}
\]

(3)

where \(C_{11}, C_{12}, \) and \(C_{44}\) are the elastic constants, and \(S_{11}, S_{12}, \) and \(S_{44}\) are elements in the compliance matrix. The bulk moduli of MoNbTaVW and W obtained by the Voigt–Reuss–Hill scheme are 216.59 GPa and 324.53 GPa, respectively. The experimental lattice constants of MoNbTaVW and W that were measured under pressure, and those obtained from the DFT estimation based on the BM3-EOS, are shown in Fig. 3(b). As seen in the figure, the DFT simulations on the structural and mechanical properties are very close to the experimental observation. At 0 K, the simulated shear modulus (\(G\)), Young's modulus (\(E\)), and Poisson's ratio (\(\nu\)) for MoNbTaVW are 57.62 GPa, 158.69 GPa, and 0.3750, respectively. The Vickers hardness, \(H_v\), which was calculated by using Tian’s model [47], is 3.72 GPa.

The azimuthally unrolled diffraction images as a function of direction angle for MoNbTaVW and W before compression, at ~5 GPa up to ~20 GPa, and after releasing pressure are shown in Fig. 4(a). The diffraction lines of Au are marked at the top of the figure. Curved diffraction lines under pressure indicate the existence of compressive stresses which lead to lattice strain. Under 20 GPa, curvature of the diffraction peaks for MoNbTaVW is much stronger than that of W, which represents larger lattice strain under high pressure. The alternative change of intensity on each diffraction line (peak) is induced by the development of dislocations under shear stress. Comparing with W, the texture of MoNbTaVW is much stronger, which suggests that the dislocation behavior is much more active in MoNbTaVW, and the dislocation density is consequently higher. Both MoNbTaVW and W form in the BCC structure with strong lattice strain and texture appearing at ~5 GPa. With the increase of pressure, no significant change in the diffraction lines was obtained in
The equation for the lattice strain and $d$ spacing measured by X-ray diffraction in this system can be described as

$$d_m(hkl, \psi) = d_0(hkl)[1 + Q(hkl)(1 - 3\cos^2 \psi)]$$  \hspace{1cm} (5)

where $d_m(hkl, \psi)$ is the measured $d$-spacing, $d_0(hkl)$ is the hydrostatic $d$-spacing, $\psi$ is the angle between the diffracting plane normal and the loading axis, and $Q(hkl)$ is the lattice strain parameter caused by deviatoric stress component, which is given by

$$Q(hkl) = (t/3)[\alpha(2G_h(hkl))^{-1} + (1 - \alpha)(2G_v)^{-1}]$$  \hspace{1cm} (6)

where $G_h(hkl)$ and $G_v$ are the shear moduli of the aggregate under Reuss (isostress) and Voigt (isostrain) approximations, respectively. They are expressed as

$$[2G_h(hkl)]^{-1} = [S_{11} - S_{12} - 3(S_{11} - S_{12} - S_{44}/2)t'(hkl)],$$

$$t'(hkl) = (h^2k^2 + l^2k^2 + h^2l^2)[(h^2 + k^2 + l^2)^2],$$  \hspace{1cm} (7)

and

$$(2G_v)^{-1} = 5S_{44}(S_{11} - S_{12})/[6(S_{11} - S_{12}) + 2S_{44}].$$  \hspace{1cm} (8)

where $S_{ij}$ are elastic compliances of material. Parameter $\alpha$ is a value between 0 and 1 describing the continuity behavior of the polycrystalline materials. If we assume isostress condition, the ratio of the differential stress to shear modulus would be $t'/G = 6Q(hkl)$, which represents the lattice strain along the direction [hkl] of each observed reflection and can be used for a first evaluation of the stress level in plastically-deforming aggregates [51]. Fig. 5(a) shows $t'(hkl)/G$ for MoNbTaVW and W. These values of MoNbTaVW are about three times larger than those of W, indicating a much higher stress level in the former sample. Our synchrotron XRD rDAXC experiment, with an average particle size of ~1 µm, showed that both MoNbTaVW and W started to yield at a pressure of ~5 GPa. The $t'/G$ ratios for both samples increase from 0 to 5 GPa and then remain stable in the pressure range between 5 GPa and 20 GPa. This result indicates that the deformation remains elastic when the pressure is below 5 GPa, while plastic deformation begins above 5 GPa. In both samples, the ratio $t'(200)/G$ has the smallest value, indicating that this is the softest plane and supports the lowest stress, while a larger lattice stain anisotropy is observed in MoNbTaVW. Fig. 5(b) compares the average differential stress ($t$) for MoNbTaVW and W based on the ratio $t'/G$, where the shear moduli, $G$, under different pressures were obtained by the Voigt–Reuss–Hill averaging scheme based on DFT calculations. The differential stresses of both materials increase rapidly when the pressure is below 5 GPa and then increase slowly in the pressure range between 5 GPa to ~20 GPa. MoNbTaVW supports a differential stress of ~2.35 GPa when it starts to yield at ~5 GPa. It reaches 3.0 GPa when the pressure is about 19.4 GPa. Pure W displays a yield strength of ~1.5 GPa and it reaches 2.15 GPa at 19.3 GPa. Furthermore, the yield strength of MoNbTaVW is about 1.5 times higher than that of Xiong et al. [52] measured the stress of W with a particle size of 4–6 µm by non-hydrostatic compression using the same technique. The results showed that the stress of W reaches ~2 GPa when the pressure is 20 GPa [52], which is consistent with our observation. It is well known that atoms of different elements are distributed randomly in the crystal lattice of high entropy alloy, the different atomic properties and interactions make it hard for atoms to diffuse, which induce the high strengthening of the alloy. On the other hand, the elements contained in MoNbTaVW have high strength in their pure metal, which may enhance the property of alloy as well. Specifically, in this research, we further found that the texture of MoNbTaVW becomes stronger under high pressure, which indicates stronger dislocation interactions under stress. The details are described in next section.

Under uniaxial compression, differential stress impose both elastic and plastic strain in the specimen. The variations in peak positions with azimuthal angle represent elastic strain, while the...
plastic strain induced lattice preferred orientation (LPO), or texture, is manifested by variations in peak intensity with azimuth in diffraction patterns. The lattice strain of the specimen was fitted with the “Radial Diffraction in the DAC” model in MAUD and \( Q(hkl) \) could be directly obtained. Crystallographic textures were fitted using the E-WIMW algorithm, an extension of the WIMW algorithm [53], with an orientation distribution function (ODF) resolution of 15° and assuming cylindrical symmetry about the compression direction. The ODF was subsequently smoothed with 7.5° Gauss filter in Beartex to remove artifacts from the ODF resolution [54]. Finally, inverse pole figures (IPF) that show the relationship between crystallographic directions of crystallites to the compression direction were generated. For cubic crystal symmetry, a fundamental sector of the IPF between 001, 110, and 111 is sufficient to represent the whole ODF. Pole densities are given in multiples of a random distribution (m.r.d.), where mrd = 1 corresponds to a random distribution and an m.r.d. of infinity corresponds to a single-crystal texture.

IPFs of the compression direction were used to represent the texture. Fig. 6 shows the texture development of both the MoNbTaVW and pure W samples under pressure. Multiples of a random distribution (m.r.d.), which represent pole densities, under various pressure are marked by colors from blue (weak) to red (strong). At ambient conditions, both MoNbTaVW and W displayed a nearly random texture. With the increase of pressure, both samples developed a texture characterized by two maxima in the 100 and 111 directions and a minimum at 110. This is consistent with previous radial X-ray diffraction studies on W [52]. This texture also agrees with compression textures reported for BCC metals and is attributed to dominant slip on \( \{110\} <111> \) [55]. Very recently, F. Maresca’s group [10] claimed that the edge dislocation plays an important role in the strengthening of BCC HEAs, based on both experimental and computational results, which are also consistent with the observations in this work. The maximum IPF of MoNbTaVW increased to 4.46 m.r.d. when the applied pressure was 19.4 GPa, while the maximum IPF of pure W increased to 1.56 m.r.d. at a pressure of 19.3 GPa. The stronger texture of MoNbTaVW under 20 GPa indicates higher dislocation activity, resulting in higher plastic deformation of the material [26,27]. Thus this is the first time in situ observation of the strength enhancement of MoNbTaVW under stress along with the nucleation of dislocations. The formation of a strong texture is an effective way to improve strength, the similar discovery has also been reported in Mg alloys [56] and Al alloys [57]. The IPF of both
samples during decompression are shown at the top of Fig. 6. The texture of both samples has changed, as compared to that before compression. The maximum IPF of MoNbTaVV after releasing the pressure is 1.81 m.r.d., while that for pure W is 1.78 m.r.d., which indicates that part of the dislocation activity will recover when the pressure is released.

4. Conclusion

In this work, we have demonstrated a unique experimental method to study the deformation behavior of a high-entropy alloy MoNbTaVV under compression conditions in situ, by using synchrotron XRD and DAC techniques. Pure W metal was used as a reference sample. XRD patterns under various pressures illustrated that MoNbTaVV is more capable of resisting high pressure, and the strength of MoNbTaVV we obtained is about 1.5 times higher than that of pure W under compression. Due to the shear stress produced by DAC forces, both MoNbTaVV and W deform plastically under high pressure. The dislocation-induced texture in MoNbTaVV is much stronger than that of W. The origin of the high strength and phase stability in MoNbTaVV, and quite likely in all HEAs, resides in these strong active dislocations. This in situ method can also be used in other HEA dislocation slip systems, which will provide further understanding of the mechanism responsible for their excellent mechanical properties and help to design ultra-high-performance alloy materials required in various fields.

CRediT authorship contribution statement

Congyan Zhang: Conceptualization, Methodology, Data curation. Binbin Yue: Methodology, Data curation. Uttam Bhandari: Theoretical simulation. Oleg N. Starovoitov: Sample preparation. Yan Yang: Sample preparation. David P. Young: Resources. Jinyuan Yan: Resources. Fang Hong: Conceptualization, Original draft preparation. Shizhong Yang: Conceptualization, Supervision. All authors: Review and editing the manuscript.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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