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## Effects of water on P-V-T equation of state of pyrope

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## ABSTRACT

High-pressure single-crystal/powder synchrotron X-ray diffraction was carried out on a hydrous pure magnesium pyrope ( $\text{Mg}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) containing 900 ppmw  $\text{H}_2\text{O}$ , synthesized at 4.0 GPa and 1300 K. The pressure-volume ( $P$ - $V$ ) single-crystal data from room pressure to 9.81 GPa at ambient temperature were fitted by a third-order Birch-Murnaghan equation of state (BM-EoS) yielding a unit-cell volume of  $V_0 = 1505.14 \pm 0.38 \text{ \AA}^3$ , an isothermal bulk modulus of  $K_0 = 160 \pm 3 \text{ GPa}$  and its pressure derivative  $K'_0 = 5.2 \pm 0.4$ . When fixing  $K'_0 = 4.0$ , the data yielded  $V_0 = 1504.58 \pm 0.32 \text{ \AA}^3$  and  $K_0 = 166 \pm 2 \text{ GPa}$ . The pressure-volume-temperature ( $P$ - $V$ - $T$ ) EoS of the synthetic hydrous pyrope was also measured at temperatures up to 900 K and pressures up to 16.75 GPa, using a diamond anvil cell in conjunction with *in situ* synchrotron angle-dispersive powder X-ray diffraction. The  $P$ - $V$  data at room temperature and in a pressure range of 0.0001–14.81 GPa were then analyzed by a third-order BM-EoS and yielded  $V_0 = 1505.35 \pm 0.25 \text{ \AA}^3$ ,  $K_0 = 161 \pm 2 \text{ GPa}$ ,  $K'_0 = 5.0 \pm 0.3$ . With  $K'_0$  fixed to 4.0, we also obtained  $V_0 = 1505.04 \pm 0.29 \text{ \AA}^3$  and  $K_0 = 167 \pm 1 \text{ GPa}$ . Consequently, we fitted the  $P$ - $V$ - $T$  data with the high-temperature third-order BM-EoS approach and obtained the thermoelastic parameters of  $V_0 = 1505.4 \pm 0.3 \text{ \AA}^3$ ,  $K_0 = 162 \pm 1 \text{ GPa}$ ,  $K'_0 = 4.9 \pm 0.2$ , the temperature derivative of the bulk modulus  $(\partial K_0 / \partial T)_P = -0.018 \pm 0.004 \text{ GPa K}^{-1}$ , and the thermal expansion coefficient at ambient conditions  $\alpha_0 = (3.2 \pm 0.1) \times 10^{-5} \text{ K}^{-1}$ . These properties were consistent with the thermal pressure EoS analysis. These new results on hydrous pyrope were also compared with previous studies of anhydrous pyrope. The main effect of hydration on pyrope is to decrease  $K_0$  and increase  $K'_0$  by increasing the vacancies or unoccupied volume in the structure. The entire dataset enabled us to examine the thermoelastic properties of important mantle garnets and this data has further applications for modeling the  $P$ - $T$  conditions in the upper mantle of the Earth's interior using deep mineral assemblages.

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## 1. Introduction

Silicate garnets are nesosilicates with the general formula  $\text{X}_3\text{Y}_2(\text{SiO}_4)_3$ , where the eight-coordinated dodecahedral X sites are usually occupied by divalent cations (typically Mg, Fe, Mn, or Ca) and the six-coordinated octahedral Y sites by trivalent cations (typically Al, Fe, or Cr). These octahedral/tetrahedral sites form a three-dimensional corner-sharing network which defines interstitial dodecahedral divalent metal sites with eightfold coordination (Smyth et al., 2000). Garnets are widespread minerals in the upper mantle and transition zone of Earth, comprising of up to 40% of the pyrolite composition volume and up to 70% of the eclogitic composition (Akaogi and

Akimoto, 1977; Anderson and Bass, 1984; Irifune and Ringwood, 1987; Ita and Stixrude, 1992; Dymshits et al., 2014). Garnets are also important components of the subducted oceanic crust (Irifune and Ringwood, 1993; Kubo et al., 2002) as stable phases in a wide range of pressures and temperatures, and play a fundamental role in many high-pressure and high-temperature petrologic processes (Saltzer et al., 2001; Keshav et al., 2007). As the principal mineral end member of the garnet group, pyrope ( $\text{Mg}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) is widely accepted as playing an important role in understanding the properties of the upper mantle and transition zone (Sinogeikin and Bass, 2002a,b; Frost, 2008; Fumagalli and Klemme, 2015). Garnet lherzolite models of the upper mantle can contain a pyrope volume about 15% (Boyd et al., 2004; Hunter and Smith, 1981). Pyrope forms a complete solid solution with  $\text{MgSiO}_3$ -majorite (Gasparik, 2000), another garnet found in the upper mantle and transition zone of the Earth. Natural garnets from eclogite xenoliths are usually pyrope-rich (Lu and Keppeler, 1997). Therefore, accurate knowledge of the thermoelastic properties of

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pyrope is directly relevant for deducing appropriate compositional models, seismic tomographic images, and the velocity and density profiles of the Earth's interior (e.g. Duffy and Anderson, 1989; Weidner and Wang, 2000).

The nominally anhydrous mineral phases in the Earth's upper mantle and transition zone (410–660 km depth) may serve as a large internal reservoir of water which has profound implications for Earth's evolution as a water planet (Ohtani, 2005; Beran and Libowitzky, 2006; Tenner et al., 2009). Water plays important roles in the phase transformation kinetics in the Earth's interior, which affects the mantle dynamics (e.g., Kubo et al., 1998). Trace amounts of dissolved hydrogen defects in nominally anhydrous mantle phases influence the physical properties of mantle materials, such as rheology (e.g., Chen et al., 1998; Mei and Kohlstedt, 2000; Jung and Karato, 2001; Kavner, 2003; Karato, 2006), elasticity (e.g., Jacobsen, 2006), and electrical conductivity (e.g., Karato, 1990; Huang et al., 2005). Much effort has been made estimating the water storage capacity of nominally anhydrous mineral phases to determine factors controlling water incorporation into the structure (e.g., Rossman and Aines, 1991; Kohlstedt et al., 1996; Rossman, 1996; Lu and Keppeler, 1997; Withers et al., 1998; Smyth et al., 2003, 2007; Skogby, 2006; Mookherjee and Karato, 2010; Tenner et al., 2012). In the context of water storage at high pressures, garnet is a particularly important phase because grossular ( $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) is known to be capable of dissolving up to 20.80 wt%  $\text{H}_2\text{O}$  (Passaglia and Rinaldi, 1984; O'Neill et al., 1993) and significant water content has been found in pyropic garnet from xenoliths (Bell and Rossman, 1992). Water content in garnet also can be used to place constraints on water fugacities (Aines and Rossman, 1984). Trace element zoning in garnet may be used to investigate the P-T paths in metamorphic rocks (Hickmott et al., 1987; Hickmott, 1989). Hydrogen zonation in garnet may be an important source of information about the metamorphic processes that occur during crystal growth (Hickmott, 1989). Since garnet increases in abundance from about 5% volume at a 150 km depth to around 30% at a 650 km depth (Ringwood, 1991), it is important to know whether this phase can dissolve large amounts of water throughout its compositional and P-T stability range. Previous studies have revealed that hydroxyl occurrence in nominally anhydrous mantle phases is closely related to cation vacancy defects (e.g., Ingrin and Skogby, 2000; Skogby, 2006). Moreover, water may be incorporated in garnets as  $\text{OH}^-$  defects associated with charge balancing or oxidation-reduction reactions, or it may substitute Si in the hydrogarnet substitution (Lu and Keppeler, 1997; Withers et al., 1998; Mookherjee and Karato, 2010). Therefore, the hydrous component in garnet has important geological implications for the Earth's mantle, and it is critical to understand the state of water and its role in the structure of garnets in the Earth's interior.

To date, the elasticity of pyrope has been extensively studied using both multi-anvil apparatus and the diamond anvil cell (e.g., Hazen and Finger, 1978; Sato et al., 1978; Levien et al., 1979; Leitner et al., 1980; Leger et al., 1990; Conrad et al., 1999; Zhang et al., 1998; Chen et al., 1999; Wang and Ji, 2001; Sinogeikin and Bass, 2000, 2002a,b; Li et al., 2011). Up to now, most of the pyrope studies have been limited to either high pressure and room temperature or ambient pressure and high temperature, however, there have been few studies that focus on the thermoelastic properties of pyrope (Bonczar and Graham, 1977; Wang et al., 1998; Sinogeikin and Bass, 2002a,b; Gwanmesia et al., 2006; Zou et al., 2012; Lu et al., 2013; Du et al., 2015). Furthermore, to our knowledge, there are no reports about the thermoelasticity of hydrous pyrope at simultaneously high pressure and high temperature, which hinders the accurate determination of appropriate compositional models and density profiles of the Earth's upper mantle.

Here, we investigated the pressure-volume-temperature (*P-V-T*) relations of a synthetic hydrous pyrope at high pressure and high temperature up to 17 GPa and 900 K, using a diamond anvil cell combined with *in situ* synchrotron radiation angle-dispersive X-ray diffraction. The thermoelastic properties of the hydrous pyrope were obtained by fitting the present *P-V-T* data to the high-temperature Birch-Murnaghan (HTBM) EoS and thermal pressure EoS. We also discuss our results with respect to previous reports of the thermoelastic properties of anhydrous pyrope, and evaluate the high pressure-temperature and hydrogen effects on pyrope to aid the current understanding of Earth's deep upper-mantle mineralogical models.

## 2. Sample and experimental methods

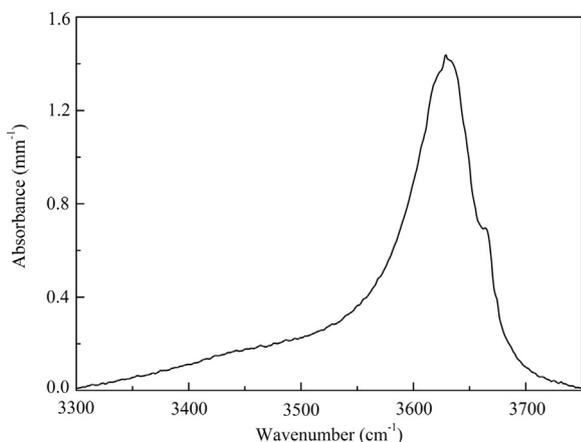
### 2.1. Sample

The synthesis of hydrous pyrope was carried out using a multi-anvil pressure apparatus (YJ-3000T), at the Institute of Geochemistry, Chinese Academy of Sciences, Guiyang, China. Details of this experimental set-up are described elsewhere by Xie et al. (1993). The pressurization system of this press consisted of six WC anvils, with their tips truncated to  $23.5 \times 23.5 \text{ mm}^2$ , which were simultaneously pushed by six hydraulic rams to generate high pressure in the experimental assembly (Fan et al., 2013). The pressure in the sample chamber was calibrated using a quartz-coesite phase transition and the high-pressure melting curve of copper, with a pressure measurement error margin of less than 1.5%. The temperature in the sample chamber was measured using a Pt-Pt<sub>90</sub>Rh<sub>10</sub> thermocouple, with an uncertainty value less than 5 K (Xie et al., 1993, 2002). The starting materials used in the synthesizing experiments were stoichiometric amounts of high purity magnesium oxide (MgO), aluminum oxide ( $\text{Al}_2\text{O}_3$ ) and silica ( $\text{SiO}_2$ ). The mixture was then melted at 1 atm and 1700 K, which produced a homogeneous glass after quenching. The homogeneous glass was crushed and ground into a fine powder in acetone and then encapsulated in platinum capsules with 10 wt% of deionised water. The synthesis was carried out at 4.0 GPa and 1300 K with a run duration of 48 h, and perfectly clear and inclusion-free single crystals of pyrope were picked from the charge. The ambient X-ray diffraction data were collected using a D/Max-2200 X-ray diffractometer with graphite crystal monochromator and Cu K $\alpha$  radiation. The ambient powder X-ray spectrum of pyrope was indexed according to the standard spectra (JCPDS 87-1093), confirming that the structure of the synthetic pyrope was cubic, and belonged to the *Ia3d* space group. The electron probe microanalysis further confirmed that the synthetic sample was a single phase with the composition as follows (in wt%): MgO, 29.9(3);  $\text{Al}_2\text{O}_3$ , 24.9(2);  $\text{SiO}_2$ , 44.7(2), which can be also written in term of formula unit as  $\text{Mg}_{3.01}\text{Al}_{2.00}\text{Si}_{3.01}\text{O}_{12}$ .

Several crystals were mounted individually in epoxy resin so that doubly-polished crystal slabs could be prepared. After polishing, the crystal slabs were extracted from the resin and cleaned using  $\text{CCl}_4$ . An electronic micrometer with a 1  $\mu\text{m}$  precision was used to measure the sample thickness, which ranged between 300 and 500  $\mu\text{m}$ . A Nicolet 5700 FTIR spectrometer coupled with a microscope was used to analyze the OH contents of X-ray-oriented, faceted single crystals using a KBr beam-splitter and a liquid-nitrogen cooled MCT-A detector. Measurements were performed through optically clean, inclusion-free, and crack-free areas under a continuous dry air flush. Where samples were large enough, we employed a focused 100  $\mu\text{m}$  spot size on the crystal surface through redundant aperturing. Smaller apertures were used to analyze areas down to  $40 \times 40 \mu\text{m}$ . Our synthesized pyropes have an asymmetric peak in the absorption spectrum centered at  $3630 \text{ cm}^{-1}$  (Fig. 1), which corresponds exactly to those in the OH spectra of synthetic pyropes of previous studies (Geiger et al., 1991; Withers et al., 1998; Mookherjee and Karato, 2010). The water contents were computed from integrated absorbances using the calibration of Bell et al. (1995) for pyrope, which showed that the water content of this hydrous pyrope sample was about 900 ppmw.

### 2.2. Room-temperature and high-pressure single-crystal X-ray diffraction experiment

Before loading into the diamond anvil cell, the pyrope crystal was examined in air. The refined unit-cell parameters constrained to cubic symmetry are reported in Table 1. The *in situ* room temperature and high-pressure synchrotron single-crystal X-ray diffraction experiments were carried out at the BL15U1 beamline using angle-dispersive diffraction with diamond-anvil cells at the Shanghai Synchrotron Radiation Facility (SSRF). A symmetric-type diamond anvil cell equipped with 500  $\mu\text{m}$  diamond culets was used for pressure generation. A gasket made of stainless steel foil (type T301) with pre-indented thickness of  $\sim 55 \mu\text{m}$  and a center hole of 200  $\mu\text{m}$  in diameter served as the sample chamber. The 4:1 methanol-ethanol mixture was used as a pressure-transmitting medium, which is hydrostatic up to 10 GPa as



**Fig. 1.** FTIR spectra of synthetic pyrope garnet for the wave-number range of 3300–3750  $\text{cm}^{-1}$ .

**Table 1**

Unit cell parameters of hydrous pyrope from single-crystal X-ray diffraction data at high pressure and room temperature.

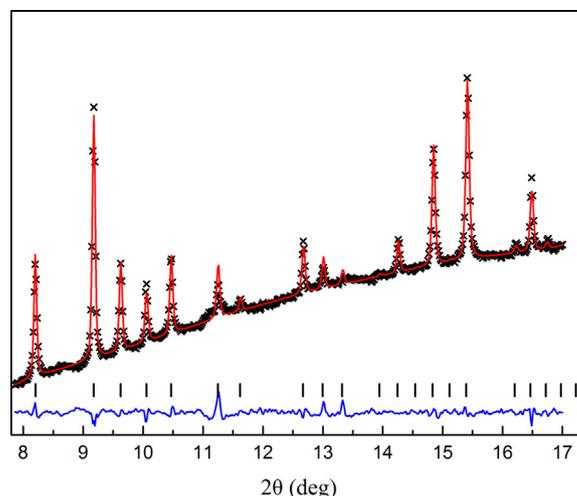
P (GPa)	V ( $\text{\AA}^3$ )
0.0001	1505.24(8)
0.45(3)	1500.52(7)
1.32(11)	1492.75(8)
2.28(37)	1484.54(8)
3.44(28)	1474.38(9)
4.73(36)	1463.56(8)
5.62(47)	1457.87(10)
6.47(38)	1451.35(8)
7.59(43)	1442.13(10)
8.73(52)	1433.85(9)
9.81(48)	1427.22(10)

Numbers in parenthesis represent standard deviations.

demonstrated by Piermarini et al. (1973) and Angel et al. (2007). A ruby chip was loaded as a pressure calibrant together with the hydrous pyrope sample (about  $50 \times 50 \times 25 \mu\text{m}$ ) in the sample chamber. Ruby fluorescence spectra were collected before and after each collection of X-ray diffraction data, and the positions of the R1 and R2 peaks were determined by fitting them with Lorentzian functions. The pressure was calculated from the fitted R1 and R2 peak positions using the method of Mao et al. (1978). Diffraction images were collected using MAR-165 charge coupled device (CCD) detector, placed at a distance of approximately 180 mm to the sample. The detector geometry parameters were calibrated using a  $\text{CeO}_2$  diffraction standard. The X-ray beam was monochromatized to a wavelength of 0.6199  $\text{\AA}$  and focused down to  $2 \times 3 \mu\text{m}^2$  area. Diffraction data were collected while the diamond anvil cell rotated around the vertical axis of the instrument ( $\omega$ -axis) from  $-12$  to  $+12^\circ$ , with a typical exposure time of 0.5 s/ $^\circ$ . Diffraction images were analyzed using the GSE\_ADA/RSV software package (Dera et al., 2013). Then, the unit-cell parameters of hydrous pyrope were calculated by a least squares technique using Unifit software (Holland and Redfern, 1997). Each diffraction pattern has at least 30 good single crystal diffraction spots. Except the single crystal diffraction spots of diamond, all the other single crystal diffraction spots could be successfully indexed using the cubic symmetry of pyrope. In the calculation, at least 11 sample diffraction spots were used to refine the unit-cell parameters: (400), (420), (332), (422), (431), (521), (611), (620), (444), (640), and (642).

### 2.3. High-temperature and high-pressure powder X-ray diffraction experiment

High-temperature and high-pressure experiments were carried out by using a modified Merrill-Bassett type diamond-anvil cell. The culet-size of the diamonds, sample chamber of the gaskets and the pressure-transmitting medium were the same as those in the single crystal



**Fig. 2.** Le Bail profile fitting of the hydrous pyrope diffraction profiles at 13.21 GPa and 900 K. Observed spectra (black line), fitted spectra (red solid line), difference plot (blue solid line) and Bragg peak positions (tick marks) are shown. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

diffraction experiment. The hydrous pyrope powders were slightly pressed between two opposing diamond anvils to form an approximately  $25 \mu\text{m}$  thick disk, and a piece of the sample about  $100 \mu\text{m}$  in diameter was loaded into the sample chamber. The cell pressure was determined using the equation of state of gold (pressure marker) as proposed by Fei et al. (2007). Heating was conducted using a resistance-heating system, and the temperature was measured using a  $\text{Pt}_{90}\text{Rh}_{10}\text{-Pt}_{100}$  thermocouple attached to the pavilion of the diamond anvil. We first compressed the sample up to 10 GPa and then increased the temperature up to 900 K. Heating was maintained at 900 K for about 15 min in order to minimize the effect of any stress that could develop during cold compression. Following this, the temperature was lowered down to 300 K in 200 K steps. At each P-T condition, an X-ray diffraction pattern was collected after the experiment temperature was maintained for  $\sim 600$  s. The typical exposure time for collecting the diffraction patterns of the sample and the pressure marker was 600 s. Details of the experimental setup and cell assembly are described in Fan et al. (2010).

*In situ* high temperature and high pressure powder X-ray diffraction experiments were conducted at the 4W2 beamline of the Beijing Synchrotron Radiation Facility (BSRF). An image plate detector (MAR-345) was used to collect diffraction patterns. The wavelength of the monochromatic X-ray beam was 0.6199  $\text{\AA}$  and calibrated by scanning through the Mo metal *K*-absorption edge. The X-ray beam was focused to a beam size of  $20 \times 30 \mu\text{m}^2$  full-width at half maximum (FWHM) by a pair of Kirkpatrick-Baez mirrors. The tilting and rotation of the detector relative to the incident X-ray beam was calibrated using cerium dioxide ( $\text{CeO}_2$ ) powder as the X-ray diffraction standard. The sample-detector distance was calculated from the powder  $\text{CeO}_2$  diffraction pattern at ambient conditions. The collected diffraction patterns were integrated to generate the conventional one-dimensional diffraction profiles using Fit2D (Hammersley et al., 1996). Fig. 2 shows a typical fitting of the full X-ray diffraction pattern of hydrous pyrope at 10.79 GPa and 900 K. Analyses of all the patterns were carried out using the full profile-fitting technique implemented in the EXPGUI/GSAS software package (Larson and Von Dreele, 2000; Toby, 2001). The refinement of the peak positions and extraction of the cell parameters were achieved by reducing full diffraction patterns following the Le Bail method (Le Bail et al., 1988). Precision of the volume determination for hydrous pyrope was estimated from the full spectrum fitting (Le Bail refinement) of X-ray diffraction profiles.

### 3. Results and discussion

The unit-cell parameters of hydrous pyrope refined from single-crystal and powder X-ray diffraction are summarized in Table 1

and 2, respectively. The room temperature and high pressure single-crystal X-ray diffraction data were fitted to the third-order BM-EoS to derive bulk modulus ( $K_0$ ) and its pressure derivative ( $K'_0$ ) of hydrous pyrope. For the high temperature and high pressure powder X-ray diffracton data, first we fitted the compression  $P$ - $V$  data at the 300 K isotherm to the BM-EoS for comparison, and then applied the high-temperature BM-EoS and thermal pressure EoS approach to derive the thermoelastic parameters from the measured  $P$ - $V$ - $T$  data.

### 3.1. Room-temperature Birch-Murnaghan equation of state (BM-EoS)

The pressure-volume ( $P$ - $V$ ) data from the single-crystal (Table 1) and powder sample (Table 2) were fitted to a third order BM-EoS:

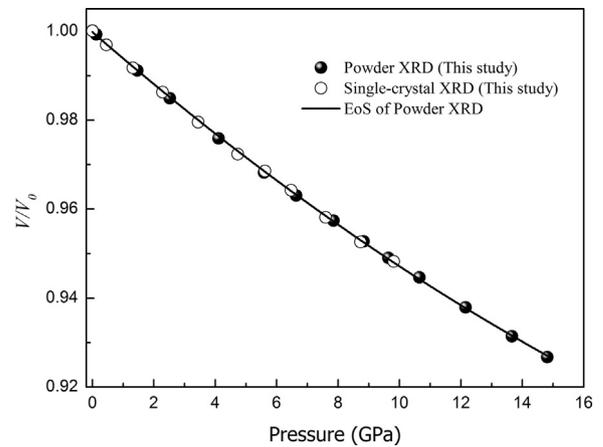
$$P = (3/2) K_0 [(V_0/V)^{7/3} - (V_0/V)^{5/3}] \times \{1 + (3/4)(K'_0 - 4) \times [(V_0/V)^{2/3} - 1]\} \quad (1)$$

where  $V_0$ ,  $K_0$ , and  $K'_0$  are the unit-cell volume, isothermal bulk modulus and its pressure derivative at ambient conditions, respectively. The fitting without any constraints yielded  $V_0 = 1505.14 \pm 0.38 \text{ \AA}^3$ ,  $K_0 = 160 \pm 3 \text{ GPa}$ ,  $K'_0 = 5.2 \pm 0.4$  for the single-crystal sample and  $V_0 = 1505.35 \pm 0.25 \text{ \AA}^3$ ,  $K_0 = 161 \pm 2 \text{ GPa}$ ,  $K'_0 = 5.0 \pm 0.3$  for the powder sample. With fixed  $K'_0$  at 4 (i.e. the second order BM-EoS), the fitting yielded  $V_0 = 1504.58 \pm 0.32 \text{ \AA}^3$  and  $K_0 = 166 \pm 2 \text{ GPa}$  for the single-crystal and  $V_0 = 1505.04 \pm 0.29 \text{ \AA}^3$  and  $K_0 = 167 \pm 1 \text{ GPa}$  for the powder. The single-crystal and powder data show excellent agreement with each other. Fitting the combined data yielded:  $V_0 = 1505.02 \pm 0.23 \text{ \AA}^3$ ,  $K_0 = 161 \pm 2 \text{ GPa}$ ,  $K'_0 = 5.2 \pm 0.3$  (without any constraints) and  $V_0 = 1504.33 \pm 0.31 \text{ \AA}^3$ , and  $K_0 = 167 \pm 1 \text{ GPa}$  (with fixed  $K'_0 = 4$ ). Fig. 3 shows the volume compression ( $V/V_0$ ) of hydrous pyrope as a function of pressure ( $P$ ) and the derived equation of state from the combined data (without any constraints). From Fig. 3, we can also see that the volume compressions of hydrous pyrope are consistent before and after heating (Table 2). In addition, although the water content was difficult to determine after the high-pressure and temperature powder X-ray diffraction measurements of the hydrous pyrope sample in this study, Dai et al. (2012) determined the water content before and after measurements of the electrical conductivity of hydrous garnet, indicating a water loss of less than 10%. The pressure range in this study ( $\sim 15 \text{ GPa}$ ) is significantly higher than Dai et al. (2012) ( $\sim 4 \text{ GPa}$ ), while the temperature range in this study ( $\sim 900 \text{ K}$ ) is obviously lower than Dai et al. (2012) ( $\sim 1273 \text{ K}$ ). Therefore, we infer that there was no obvious water loss during the experimental pressure-temperature range in this study.

**Table 2**  
Unit cell parameters of hydrous pyrope from powder X-ray diffraction data at various pressure-temperature conditions.

P (GPa)	T (K)	V ( $\text{\AA}^3$ )	P (GPa)	T (K)	V ( $\text{\AA}^3$ )
Compression before heating			9.38(58)	500	1438.79(83)
0.0	300	1505.53(64)	11.28(66)	500	1425.85(75)
1.46(22)	300	1492.13(76)	13.44(54)	500	1410.82(78)
5.59(51)	300	1457.56(86)	15.26(62)	500	1399.73(85)
7.85(37)	300	1441.26(82)	2.46(54)	700	1501.16(86)
9.64(48)	300	1428.62(85)	4.52(59)	700	1484.16(78)
Compression after heating			6.77(33)	700	1466.09(86)
0.12(1)	300	1504.28(92)	8.45(45)	700	1453.06(92)
2.52(32)	300	1482.26(85)	10.28(52)	700	1439.25(81)
4.11(47)	300	1469.09(84)	12.49(54)	700	1424.36(76)
6.63(57)	300	1449.75(74)	14.55(63)	700	1411.26(79)
8.83(63)	300	1434.26(87)	16.03(47)	700	1402.62(84)
10.65(58)	300	1422.08(84)	2.98(56)	900	1506.36(77)
12.15(55)	300	1411.87(88)	5.33(46)	900	1486.09(83)
13.66(28)	300	1402.09(75)	7.42(58)	900	1469.75(84)
14.81(37)	300	1395.10(92)	9.37(52)	900	1454.95(77)
1.55(15)	500	1500.13(86)	10.79(45)	900	1444.35(83)
3.28(24)	500	1484.66(83)	13.21(36)	900	1427.76(78)
5.44(33)	500	1467.09(87)	15.44(45)	900	1413.76(82)
7.56(45)	500	1450.83(76)	16.75(64)	900	1406.12(87)

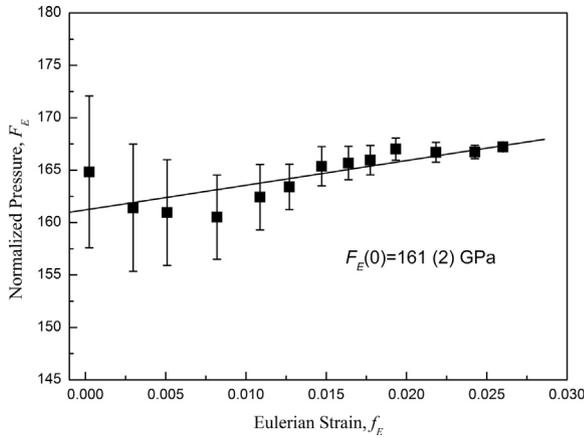
Numbers in parenthesis represent standard deviations.



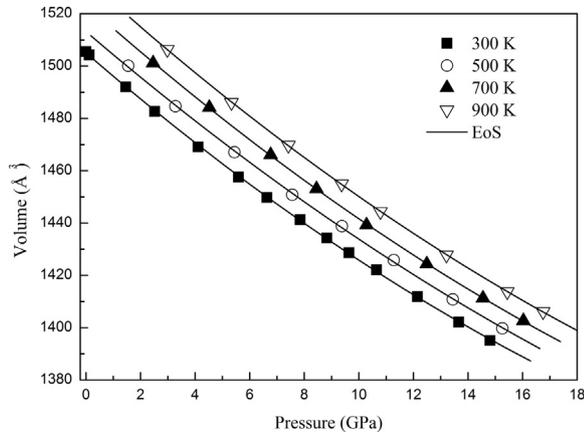
**Fig. 3.** Volume compression of hydrous pyrope at high pressure and room temperature from single-crystal X-ray diffraction experiments compared with the powder X-ray diffraction experiments in this study. The third-order BM EoS fitted with  $K_0$  and  $K'_0$  are 161 GPa and 5.0 for hydrous pyrope. The error bars of the data points are smaller than the symbols.

The second order BM-EoS yielded a significant larger  $K_0$  than the third order BM-EoS. Fig. 4 shows the volume Eulerian finite strain ( $f_E = [(V_0/V)^{2/3} - 1]$ ) versus the “normalized pressure” ( $F_E = P/[3f_E(2 - f_E + 1)^{5/2}]$ ) plot (i.e.  $F_E - f_E$  plot, (Angel, 2000)) of hydrous pyrope in this study. The weighted linear regression through the data points yielded the hydrous pyrope intercept value,  $F_E(0) = 161 \pm 2 \text{ GPa}$ , which shows excellent agreement with the isothermal bulk modulus obtained by the third-order BM-EoS ( $161 \pm 2 \text{ GPa}$ ). Furthermore, it is clear from Fig. 4 that the normalized pressure as a function of the Eulerian strain at 300 K has a positive slope, which is consistent with a value of  $K'_0$  slightly larger than 4 (Angel, 2000) shows that the third-order BM-EoS is a reasonable description of the  $P$ - $V$  data in this study (see Fig. 5).

We used a methanol-ethanol mixture with a ratio of 4:1 for the pressure medium in this study. This medium solidifies at a pressure above 10 GPa, and therefore the hydrostatic pressure environment in the sample chamber may be influenced (Piermarini et al., 1973; Angel et al., 2007). However, the sample chamber in this study was heated up to 900 K at pressures higher than 10 GPa for the relaxation of the deviatoric stress. The effect of deviatoric stress on the unit-cell volume measurements should be minimal, and this is confirmed by fitting the experimental data under hydrostatic conditions (below 10 GPa) which yields a very similar result ( $K_0 = 162 \pm 3 \text{ GPa}$ ,  $K'_0 = 4.9 \pm 0.5$ ) to the whole pressure range fitting.



**Fig. 4.** Volume Eulerian strain-normalized pressure ( $F_E - f_E$ ) plot of hydrous pyrope. The solid line represents the linear fit through the data.



**Fig. 5.** Unit-cell volume of hydrous pyrope as a function of pressure and temperature. The solid lines represent the isothermal compression curve from fitting the HTBM EoS at 300, 500, 700, 900 K with the following parameters:  $K_0 = 162 \pm 1$  GPa,  $K'_0 = 4.9 \pm 0.2$ ,  $(\partial K_0/\partial T)_P = -0.018 \pm 0.004$  GPa  $K^{-1}$  and  $\alpha_0 = (3.19 \pm 0.10) \times 10^{-5}$   $K^{-1}$ . The error bars of the data points are smaller than the symbols.

### 3.2. High-temperature Birch-Murnaghan equation of state

The  $P$ - $V$ - $T$  data (Table 2) from powder X-ray diffraction experiments were used to determine the thermoelastic properties of hydrous pyrope up to  $\sim 17$  GPa and 900 K. The high temperature third order BM-EoS was applied to our high pressure and high temperature data in the following form:

$$P = (3/2) K_{T0} [(V_{T0}/V)^{7/3} - (V_{T0}/V)^{5/3}] \times \{1 + (3/4)(K'_{T0} - 4) \times [(V_{T0}/V)^{2/3} - 1]\} \quad (2)$$

In this equation, the thermal dependences of the zero-pressure volume ( $V_{T0}$ ) and the bulk modulus ( $K_{T0}$ ) at different temperatures are expressed using the following equations:

$$V_{T0} = V_0 \exp \int_{300}^T \alpha_T dT \quad (3)$$

$$KT0 = K0 + (\partial K0/\partial T)P \times (T - 300) \quad (4)$$

where  $\alpha_T$  is the thermal expansion at ambient pressure and  $(\partial K_0/\partial T)_P$  is the temperature derivative of  $K_0$  at ambient pressure.

The hydrous pyrope thermoelastic parameters obtained in this study are shown in Table 4. Fitting our  $P$ - $V$ - $T$  data to the high temperature BM EoS yielded  $V_0 = 1505.38 \pm 0.27$   $\text{\AA}^3$ ,  $K_0 = 162 \pm 1$  GPa,  $K'_0 = 4.9 \pm 0.2$ ,  $(\partial K_0/\partial T)_P = -0.018 \pm 0.004$  GPa  $K^{-1}$  and  $\alpha_0 = (3.2 \pm 0.1) \times 10^{-5}$   $K^{-1}$ . With

$K'_0$  fixed to 4.0, we also obtained  $V_0 = 1505.22 \pm 0.28$   $\text{\AA}^3$ ,  $K_0 = 168 \pm 1$  GPa,  $(\partial K_0/\partial T)_P = -0.017 \pm 0.005$  GPa  $K^{-1}$  and  $\alpha_0 = (3.06 \pm 0.09) \times 10^{-5}$   $K^{-1}$  for hydrous pyrope. The  $K_0$  values determined here are consistent with those derived from our  $P$ - $V$  data fitting at 300 K within accepted uncertainties. We also calculated the temperature derivative of the bulk modulus extracted from each isotherm, and obtained  $(\partial K_0/\partial T)_P = -0.018 \pm 0.005$  GPa  $K^{-1}$  for hydrous pyrope, which is very consistent with the results from the whole set of  $P$ - $V$ - $T$  data available in this study  $(\partial K_0/\partial T)_P = -0.018 \pm 0.004$  GPa  $K^{-1}$ ) within their uncertainties.

Likewise, fitting the  $P$ - $V$ - $T$  data at pressures below  $\sim 10$  GPa to the high temperature BM-EoS yielded  $V_0 = 1505.33 \pm 0.31$   $\text{\AA}^3$ ,  $K_0 = 163 \pm 2$  GPa,  $K'_0 = 5.1 \pm 0.4$ ,  $(\partial K_0/\partial T)_P = -0.020 \pm 0.006$  GPa  $K^{-1}$  and  $\alpha_0 = (3.3 \pm 0.2) \times 10^{-5}$   $K^{-1}$ . These values are very consistent with all the  $P$ - $V$ - $T$  data fitting results within their uncertainties.

### 3.3. Thermal pressure equation of state

We also analyzed the  $P$ - $V$ - $T$  data using a thermal pressure approach (e.g., Anderson, 1995; Jackson and Rigden, 1996). The thermal pressure ( $\Delta P_{th}$ ) was obtained by subtracting the pressure at volume ( $V$ ) and at room temperature (derived from Eq. (1)) from the pressure measured at the same  $V$  and at temperature ( $T$ ).

$$\Delta P_{th} = P(V, T) - P(V, 300)$$

$$= \left[ \alpha K_T + \left( \frac{\partial K_T}{\partial T} \right)_V \ln \left( \frac{V_0}{V} \right) \right] \times (T - 300) \quad (5)$$

Figs. 6 and 7 show the thermal pressure of hydrous pyrope against temperature and the unit-cell volume, respectively. These data show that the thermal pressure of hydrous pyrope varies linearly with temperature and is almost independent of volume. Therefore, we assume that  $(\partial K_T/\partial T)_V = 0$  so the thermal pressures in Eq. (5) are independent of volume, an approximation that has been derived or assumed in many previous studies for mantle phases (e.g., Guyot et al., 1996; Wang et al., 1996, 1998; Anderson, 1999; Shim et al., 2000; Nishihara et al., 2004; Liu and Li, 2006; Liu et al., 2008; Fan et al., 2015). With this assumption, fitting the data in this study yielded  $K_0 = 160 \pm 2$  GPa,  $K'_0 = 4.8 \pm 0.4$ , and  $\alpha_0 = (2.9 \pm 0.2) \times 10^{-5}$   $K^{-1}$ , which is reasonably consistent with those derived by the HTBM EoS fitting (Table 4). By using the thermodynamic relation:  $(\partial K_T/\partial T)_P = (\partial K_T/\partial T)_V - \alpha K_T K'_T$ , we obtained  $(\partial K_0/\partial T)_P = -0.021(3)$  GPa  $K^{-1}$ , which is in good agreement with current analysis using the HTBM EoS (Table 4).

### 3.4. Comparison with previous studies of other garnets

Our hydrous pyrope results compared with previous studies for anhydrous pyrope are also shown in Table 3. Numerous studies on elastic properties of anhydrous pyrope have been investigated by some authors. Table 3 summarizes the  $V_0$ ,  $K_0$  and  $K'_0$  for anhydrous pyrope determined by various experimental techniques, including X-ray diffraction, ultrasonic interferometry and Brillouin scattering spectroscopy (Hazen and Finger, 1978; Sato et al., 1978; Levien et al., 1979; Leitner et al., 1980; Leger et al., 1990; Conrad et al., 1999; Zhang et al., 1998; Chen et al., 1999; Wang and Ji, 2001; Sinogeikin and Bass, 2000, 2002a,b; Li et al., 2011; Du et al., 2015). We observed a systematic expansion of the zero-pressure unit-cell volume with hydration at ambient conditions from Tables 3 and 4, which is in good agreement with many previous studies for other mantle minerals (e.g., Smyth et al., 2003; Smyth and Jacobsen, 2006; Holl et al., 2008; Ye et al., 2010, 2012). In addition, Fig. 8 shows the difference between the unit-cell volumes of the anhydrous and hydrous pyropes as a function of pressure. The anhydrous reference volume chosen for comparison in Fig. 8 was from Du et al. (2015), because they used the same pressure transmitting medium (4:1 methanol-ethanol mixture) and had a similar pressure range with this study. From Fig. 8, we see the unit-cell volumes of the anhydrous pyrope are slightly smaller than hydrous pyrope in this study at low pressures, while their unit-cell volumes become very close to each other at higher pressures due to the larger compressibility (smaller bulk modulus) of the hydrous sample. Levien et al. (1979) measured the unit-cell parameters of pyrope in a diamond anvil cell at pressures up to 5 GPa using a single crystal X-

**Table 3**  
Bulk modulus and its pressure derivative of dry pyrope and hydrous pyrope.

Sample	$K_0$ (GPa)	$K'_0$	$V_0$ ( $\text{\AA}^3$ )	Methods	References
Hydrous pyrope	167(1)	4.0 <sup>a</sup>	1505.04(29)	Powder-XRD	This study
Hydrous pyrope	161(2)	5.0(3)	1505.35(25)	Powder-XRD	This study
Hydrous pyrope	166(2)	4.0 <sup>a</sup>	1504.58(32)	Single crystal-XRD	This study
Hydrous pyrope	160(3)	5.2(4)	1505.14(38)	Single crystal-XRD	This study
Dry pyrope	172.8	3.8(1)	1503.87	Powder-XRD	Leger et al. (1990)
Dry pyrope	169.2(2)	4.4 <sup>a</sup>	1503.2	Powder-XRD	Du et al. (2015)
Dry pyrope	175(1)	4.5(5)	1503.4(5)	Single crystal-XRD	Levien et al. (1979)
Dry pyrope	171(2)	4.4(2)	1502.9(3)	Single crystal-XRD	Zhang et al. (1998)
Dry pyrope	171.32(2)	3.22	–	BLS	Conrad et al. (1999)
Dry pyrope	171.2(20)	4.1(3)	–	BLS	Sinogeikin and Bass (2000)
Dry pyrope	174.9(16)	4.7(3)	–	BLS	Jiang et al. (2004)
Dry pyrope	171(2)	5.3(4)	–	UI	Chen et al. (1999)
Dry pyrope	170.1(11)	4.9(6)	–	UI	Wang and Ji (2001)

XRD, X-ray diffraction; BS, Brillouin Light Scattering; UI, Ultrasonic interferometry.

Numbers in parenthesis represent standard deviations.

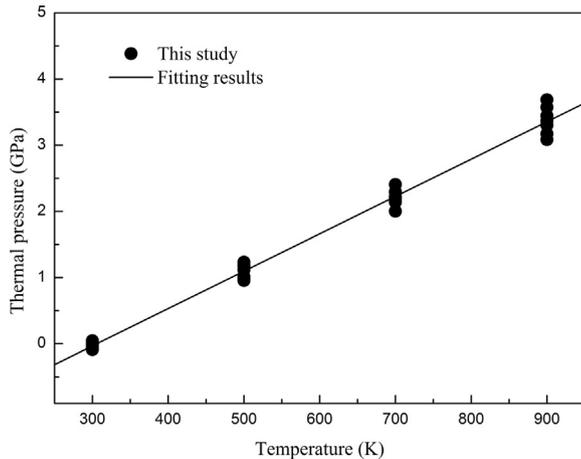
<sup>a</sup> Fixed during fitting.

**Table 4**  
Thermoelastic parameters of hydrous pyrope using the HTBM equation of state compared with dry pyrope.

Sample	$V_0$ ( $\text{\AA}^3$ )	$K_0$ (GPa)	$K'_0$	$(\partial K/\partial T)_P$ (GPa K <sup>-1</sup> )	$\alpha_0$ (10 <sup>-5</sup> K <sup>-1</sup> )	References
Dry pyrope	1503.1(5)	170(2)	5.0 <sup>a</sup>	-0.020(3)	2.58(28)	Wang et al. (1998)
Dry pyrope	–	169(2)	–	-0.019(3)	–	Sinogeikin and Bass (2002)
Dry pyrope	1502.5	172(4)	3.9 <sup>a</sup>	-0.026(2)	–	Gwanmesia et al. (2006)
Dry pyrope	1500.4(15)	167(3)	4.6 <sup>a</sup>	-0.021(9)	2.89(33)	Zou et al. (2012)
Dry pyrope	1502.8(4)	–	–	–	2.74(5)	Du et al. (2015)
Hydrous pyrope	1505.38(27)	162(1)	4.9(2)	-0.018(4)	3.19(10)	This study
Hydrous pyrope	1505.22(28)	168(1)	4.0 <sup>a</sup>	-0.017(5)	3.06(9)	This study

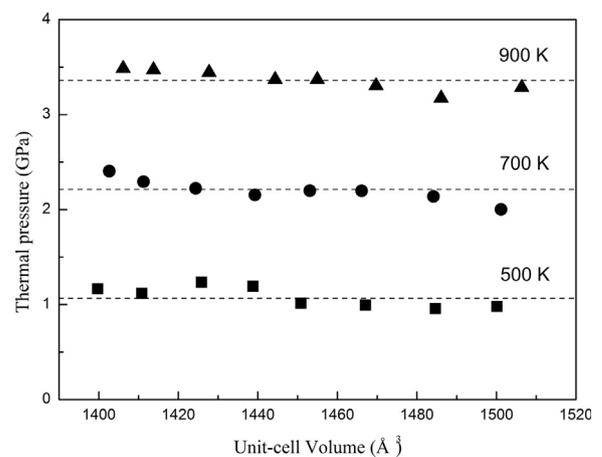
Numbers in parenthesis represent standard deviations.

<sup>a</sup> Fixed during fitting.



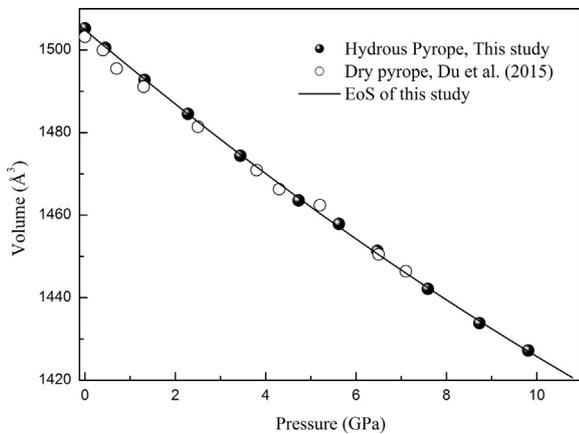
**Fig. 6.** Thermal pressure of hydrous pyrope versus temperature. Solid circles are the hydrous pyrope data in this study. The solid line is the fitting results using a thermal pressure approach.

ray diffraction method, and obtained the bulk modulus  $K_0 = 175(1)$  GPa and  $K'_0 = 4.5(5)$ . Leitner et al. (1980) determined the elastic moduli of a synthetic single crystal of pyrope using Brillouin spectroscopy, and reported  $K_0 = 175(1)$  GPa. Subsequently, Leger et al. (1990) used this  $K_0$  value and using powder X-ray diffraction to report  $K'_0 = 3.4$  for pure synthetic pyrope. Zhang et al. (1998) also investigated the equation of state and crystal structure of pyrope under hydrostatic conditions up to 33 GPa using single crystal X-ray diffraction, and obtained  $K_0 = 171(2)$  GPa and  $K'_0 = 4.4(2)$ . In addition, Conrad et al. (1999) conducted high-pressure Brillouin scattering experiments on near end-member single crystal pyrope at pressures up to 10 GPa in a diamond-anvil cell with a methanol-ethanol-water pressure medium, and calculated  $K_0$  and  $K'_0$  as 171.3 GPa and 3.22, respectively. Sinogeikin and Bass (2000) also measured the single-crystal elastic properties of synthetic pyrope up to 20 GPa using a Brillouin scattering method, and reported that the  $K_0$



**Fig. 7.** Variations of thermal pressure with the unit-cell volume at various temperatures. The dashed lines correspond to the constant values of thermal pressure for a given temperature. The data indicates that  $(\partial K_T/\partial T)_V$  is close to zero.

and  $K'_0$  were 169.4(20) GPa and 4.1(3), respectively. In contrast, studies using synthetic polycrystalline specimens and ultrasonic interferometry in a 1000 ton split-cylinder multi-anvil apparatus (Chen et al., 1999) yielded  $K_0 = 171(2)$  and  $K'_0 = 5.3(4)$ , the largest value of  $K'_0$  in the previous studies for anhydrous pyrope. Recently, Du et al. (2015) also measured the unit-cell parameters of synthetic pyrope up to 10 GPa using synchrotron X-ray powder diffraction, and yielded  $K_0 = 169.2(2)$  by fixing  $K'_0$  at 4.4 which taken from Zhang et al. (1998). From the results of these previous studies, the anhydrous pyrope bulk modulus and its pressure derivative are within the ranges of  $K_0 = 170$ –175 GPa and  $K'_0 = 3.2$ –5.3. However, we obtained the bulk modulus and its pressure derivative as  $K_0 = 161$  GPa and  $K'_0 = 5.0$  for the hydrous pyrope (about 900 ppmw) in this study. The  $K_0$  value of our hydrous pyrope was around 5–7% smaller than the anhydrous pyrope from previous studies, but its  $K'_0$  value was slightly larger. This



**Fig. 8.** Unit-cell volumes of anhydrous and hydrous pyrope at ambient temperature with pressures from 0 to about 10 GPa. The third-order BM EoS fitted with  $K_0$  and  $K'_0$  are 160 GPa and 5.2 for hydrous pyrope. The error bars of the data points are smaller than the symbols.

phenomenon is similar to the effects of water on the elastic properties of olivine, reducing  $K_0$  and increasing  $K'_0$  (Smyth et al., 2005; Jacobsen, 2006) although unchanged  $K'_0$  for hydrous olivine was also proposed (Chen et al., 2011).

In addition, as an important garnet end-member, grossular is a promising water carrier mineral in the garnet family (Rossman, 1996). Although Bolfan-Casanova et al. (2000) doubted the hydrogarnet substitution in majorite, based on the IR spectra of synthesized tetragonal  $\text{MgSiO}_3$  majorite, Pigott et al. (2015) showed that even with low-water contents, the hydrogarnet defect was likely to form in majorite, thus they inferred that majorite also incorporated water mainly through hydrogarnet substitution. Therefore, hydrogen enters the garnet structure mainly through the hydrogarnet substitution of  $\text{H}_4\text{O}_4 = -\text{SiO}_4$  (e.g., Lager et al., 2005; Jacobsen, 2006). The hydrogarnet substitution in grossular is expressed as  $\text{Ca}_3\text{Al}_2(\text{SiO}_4)_{3-x}(\text{H}_4\text{O}_4)_x$ , named hibschite ( $0 < x < 1.5$ ) and katoite ( $1.5 < x \leq 3.0$ ) (Jacobsen, 2006). A lot of studies on the elastic properties of grossular have been determined by X-ray diffraction, ultrasonic interferometry, and Brillouin scattering spectroscopy (e.g., Bass, 1989; Conrad et al., 1999; Olijnyk et al., 1991; Pavese et al., 2001; Kono et al., 2010; Gréaux et al., 2011), giving  $K_0$  values from 166 to 172 GPa. In addition, the elastic properties of a natural hibschite were determined by Brillouin spectroscopy, giving  $K_0 = 99.8$  (10) GPa (O'Neill et al., 1993). The compressibility of katoite was studied by powder (Olijnyk et al., 1991) and single-crystal (Lager et al., 2002) X-ray diffraction experiments, giving  $K_0 = 66(4)$  GPa and  $58(1)$  GPa, respectively. Thus, in going from grossular to hibschite and katoite, the bulk moduli were reduced by  $\sim 40\%$  and  $\sim 60\%$ , respectively. This is also very similar to the effects of water on the elastic properties of the pyrope garnet in this study, although  $K_0$  changed less for hydrous pyrope since there is less water content in pyrope garnet compared with grossular. In other words, the increased compressibility of garnets (e.g. pyrope, grossular) with increasing water is due to the positive volume change by introduction of the  $\text{H}_4\text{O}_4$  tetrahedron compared with the smaller and more rigid  $\text{SiO}_4$  tetrahedron (Jacobsen, 2006).

In order to obtain a consistent thermoelastic parameter set, Wang et al. (1998) refitted the entire data set of pyrope garnet at high pressure and temperature using the data from previous studies (Yagi et al., 1987; Suzuki and Anderson, 1983; and others). By fixing  $K'_0 = 5$ , they obtained  $K_0 = 170(2)$  GPa,  $(\partial K_0/\partial T)_P = -0.020(3)$  GPa  $\text{K}^{-1}$ , and  $\alpha_0 = 2.58(28) \times 10^{-5} \text{ K}^{-1}$ . Sinogeikin and Bass (2002a,b) presented the single-crystal elasticity of pure synthetic pyrope at temperatures up to 800 °C using Brillouin light scattering spectroscopy in a ceramic high-temperature cell, indicating  $K_0 = 169(2)$  GPa and  $(\partial K_0/\partial T)_P = -0.019(3)$  GPa  $\text{K}^{-1}$ . Gwanmesia et al. (2006) determined the acoustic wave velocities of synthetic polycrystalline pyrope up to 9 GPa and 1000 °C by ultrasonic interferometry combined with energy-dispersive synchrotron X-ray diffraction in a cubic-anvil DIA-type apparatus, and obtained  $K_0 = 172(2)$  GPa and  $(\partial K_0/\partial T)_P = -0.026(4)$  GPa  $\text{K}^{-1}$  by fixing  $K'_0 = 3.9$ . Recently, Zou et al. (2012) measured the thermoelastic properties of synthetic pyrope garnet at higher pressure and temperature conditions (up to

19 GPa and 1700 K) using *in situ* energy-dispersive synchrotron X-ray diffraction combined with a Kawai-type multi-anvil apparatus, and concluded that  $K_0 = 167(3)$  GPa,  $(\partial K_0/\partial T)_P = -0.021(9)$  GPa  $\text{K}^{-1}$ , and  $\alpha_0 = 2.89(33) \times 10^{-5} \text{ K}^{-1}$  for fixed  $K'_0 = 4.6$ . Du et al. (2015) also investigated the thermo-compression of a series of synthetic garnets with the pyrope, grossular, and intermediate compositions up to about 900 K and to 10 GPa using synchrotron X-ray powder diffraction with a diamond anvil cell, and obtained  $\alpha_0 = 2.74(5) \times 10^{-5} \text{ K}^{-1}$  for end-member pyrope. The results of previous studies indicate that the temperature derivative of anhydrous pyrope bulk modulus  $((\partial K_0/\partial T)_P)$  ranges from  $-0.019$  GPa  $\text{K}^{-1}$  to  $-0.026$  GPa  $\text{K}^{-1}$ , and the coefficients of thermal expansion ( $\alpha_0$ ) range from  $2.58 \times 10^{-5} \text{ K}^{-1}$  to  $2.89 \times 10^{-5} \text{ K}^{-1}$ . However, we obtained  $(\partial K_0/\partial T)_P = -0.018(4)$  GPa  $\text{K}^{-1}$  and  $\alpha_0 = 3.2(1) \times 10^{-5} \text{ K}^{-1}$  for hydrous pyrope (about 900 ppmw) in this study. The  $(\partial K/\partial T)_P$  value of the hydrous pyrope in this study is in agreement with anhydrous pyrope, whereas the  $\alpha_0$  value of the hydrous pyrope is slightly larger than anhydrous pyrope. Lu et al. (2013) measured the single-crystal elasticity of natural Fe-bearing pyrope using *in situ* Brillouin spectroscopy and X-ray diffraction at high-pressure and temperature conditions up to 20 GPa and 750 K in an externally-heated diamond anvil cell, and found  $(\partial K_0/\partial T)_P = -0.023(2)$  GPa  $\text{K}^{-1}$  for Fe-bearing pyrope, which is very consistent with the results from Wang et al. (1998)  $((\partial K_0/\partial T)_P = -0.020(3)$  GPa  $\text{K}^{-1}$ ) and Zou et al. (2012)  $((\partial K_0/\partial T)_P = -0.021(9)$  GPa  $\text{K}^{-1}$ ) for pure pyrope using a synchrotron X-ray diffraction method within their uncertainties. Therefore, based on the existing data, we believe that the temperature derivative of the pyrope bulk modulus may not be significantly affected by its iron and hydrogen content; however, hydrogen can slightly raise the thermal expansion coefficient of pyrope.

#### 4. Geophysical implications

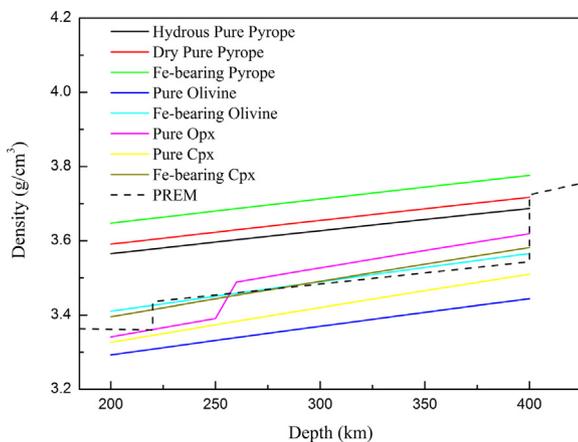
Earth's mantle mostly consists of nominally anhydrous minerals, such as olivine, pyroxenes, garnet, and their high-pressure equivalents (Williams and Hemley, 2001). Although these minerals do not contain OH groups in their formulas, they can dissolve traces of OH as point defects (Hirschmann, 2006). Investigations of natural samples suggest that these minerals may represent a major reservoir of water in the Earth (e.g. Rossman and Smyth, 1990; Skogby et al., 1990; Smyth et al., 1991; Bell and Rossman, 1992a, 1992b; Rossman, 1996; Bell et al., 2003). Pyrope occurs commonly in nature both as a metamorphic mineral and as a high-pressure phase, which is stable under upper mantle conditions (Leitner et al., 1980), and it is probably also important in the mantle-transition zone (420–670 km) depth phases (Duffy and Anderson, 1989). Furthermore, previous studies also predicted that pyrope could incorporate significant amounts of water as hydroxyl (e.g. Bell and Rossman, 1992b; Bell et al., 1995; Beran and Libowitzky, 2006). Therefore, using the newly-determined thermoelastic properties of hydrous pyrope in our present study, we calculated the density profiles of the major upper-mantle minerals.

We used the high-temperature BM-EoS to calculate the densities of the following constituent minerals at conditions corresponding to the upper mantle: pure olivine ( $\text{Mg}_2\text{SiO}_4$ ) (Guyot et al., 1996) and Fe-bearing olivine ( $\text{Mg}_{0.9}\text{Fe}_{0.1}\text{SiO}_4$ ) (Liu and Li, 2006), pure orthopyroxene ( $Pbca$ ,  $\text{MgSiO}_3$ ) (Zhao et al., 1995), pure orthopyroxene ( $C2/c$ ,  $\text{MgSiO}_3$ ) (Shinmei et al., 1999), pure clinopyroxene ( $\text{CaMgSi}_2\text{O}_6$ ) (Zhao et al., 1998) and Fe-bearing clinopyroxene (omphacite- $\text{Di}_{63}\text{Jd}_{37}$ ;  $\text{Di} = \text{Ca}(\text{Mg}, \text{Fe})\text{Si}_2\text{O}_6$ ,  $\text{Jd} = \text{NaAlSi}_2\text{O}_6$ ) (Nishihara et al., 2003), pure pyrope ( $\text{Mg}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) (Zou et al., 2012) and Fe-bearing pyrope ( $(\text{Mg}_{0.83}\text{Fe}_{0.17})_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) (Suzuki and Anderson, 1983; Lu et al., 2013; Huang and Chen, 2014), and hydrous pure pyrope ( $\text{Mg}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) (this study). As shown in previous studies, orthopyroxene with the space group  $Pbca$  transforms to high-pressure  $C2/c$  clinoenstatite at the relevant pressure and temperature conditions of the upper mantle (e.g. Shinmei et al., 1999; Bromiley and Bromiley, 2006; Yu and Wentzcovitch, 2009; Finkelstein et al., 2015), and we assumed that the OEN phase ( $Pbca$ ) transitions into the HP-CEN phase ( $C2/c$ ) at 250 km ( $\sim 8$  GPa). Therefore, we used the thermoelastic parameters of  $C2/c$  clinoenstatite by Shinmei et al. (1999) for pressures higher than 8 GPa, and  $Pbca$  orthopyroxene by Zhao et al. (1995) for pressures lower than 8 GPa in our calculations. In addition, the effect of iron incorporation on the thermoelastic properties of orthopyroxene ( $Pbca$  phase) was studied experimentally (Zhang et al., 2013). They indicated that incorporation of a small

amount of iron (about 13% ferrosilite content) in enstatite just increases the pressure derivative of the bulk modulus from about 10 to 13, but has a negligible effect on other thermoelastic parameters (Zhao et al., 1995; Zhang et al., 2013). Moreover, there is still a lack of related detailed experimental studies about the effect of iron incorporation on the thermoelastic properties of orthopyroxene (C2/c phase). Thus in our calculations, we assumed that the incorporation of a small amount of iron has a negligible effect on the thermoelastic properties of orthopyroxene (*Pbca* and *C2/c* phases).

Fig. 9 shows the density-profiles of the constituent minerals for the Earth's upper mantle region between a 200 and 400 km depth along a normal continental geotherm (Katsura et al., 2010). The PREM density-profile (Dziewonski and Anderson, 1981) is also shown in Fig. 9 for comparison. Compared with the modeled densities of anhydrous pure pyrope (Zou et al., 2012) at the P-T conditions of the upper mantle, our results show that the hydrogen effect on thermoelasticity of pyrope leads to a  $\sim 1\%$  decrease in the density. In addition, since the temperature range ( $\sim 900$  K) in the present P-V-T experiments was limited, the thermal expansion coefficient at zero-pressure was treated as a constant in the P-V-T data analysis of hydrous pyrope. This factor may lead to uncertainty in the extrapolated density profile of hydrous pyrope in the Earth's upper mantle region. Therefore, we needed to assess the possible uncertainties of the density profile of the hydrous pyrope in this study. First, we determined the temperature dependence of the thermal expansion coefficient of hydrous pyrope using the P-V-T data in this study, which yielded  $V_0 = 1505.13 \pm 0.25 \text{ \AA}^3$ ,  $K_0 = 162 \pm 1 \text{ GPa}$ ,  $K'_0 = 5.0 \pm 0.2$ ,  $(\partial K_0/\partial T)_P = -0.014 \pm 0.002 \text{ GPa K}^{-1}$  and  $\alpha_0 = (2.87 \pm 0.13) \times 10^{-5} \text{ K}^{-1}$ , and  $\alpha_1 = (0.61 \pm 0.22) \times 10^{-8} \text{ K}^{-1}$ . Using these results, we also calculated the density profile of hydrous pyrope, which shows a higher density of just  $\sim 0.15\%$ . Second, in consideration of the very minimal effect of hydrogen on the thermal expansion coefficient at ambient conditions of pyrope (Table 4), we used the thermal expansion coefficient of dry pure pyrope ( $\alpha_0 = (2.58 \pm 0.20) \times 10^{-5} \text{ K}^{-1}$ , and  $\alpha_1 = (1.02 \pm 0.46) \times 10^{-8} \text{ K}^{-1}$ ) (Zou et al., 2012) to calculate the density profile of hydrous pyrope. The resulting density profile also shows just  $\sim 0.2\%$  higher density. To sum up, we infer that if the thermal expansion coefficient at zero-pressure is treated as a constant in the P-V-T data analysis of hydrous pyrope, it may lead to very limited uncertainty in the extrapolated density profile of hydrous pyrope in the Earth's upper mantle region.

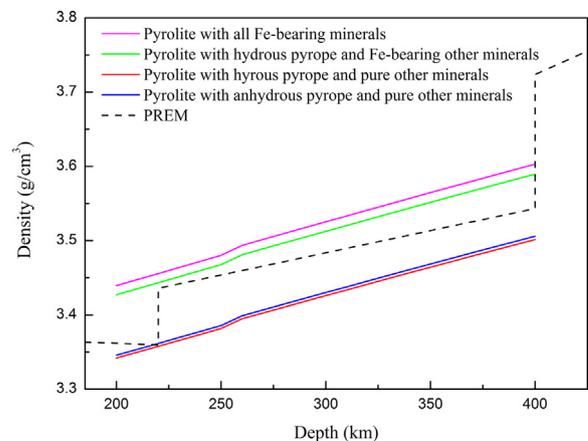
Furthermore, the density profiles of olivine, orthopyroxene, and clinopyroxene were also modeled using existing results on their thermoelasticity parameters (Suzuki and Anderson, 1983; Guyot et al., 1996; Zhao et al., 1995, 1998; Shinmei et al., 1999; Nishihara et al., 2003; Liu and Li, 2006; Lu et al., 2013; Huang and Chen, 2014). The den-



**Fig. 9.** Calculated density profiles of constituent minerals in the upper mantle between 200 and 400 km. Anhydrous pyrope (red solid line) (Zou et al., 2012), Hydrous pyrope (black solid line) (This study), Fe-bearing pyrope (green solid line) (Suzuki and Anderson, 1983; Lu et al., 2013; Huang and Chen, 2014), pure Olivine (blue solid line) (Guyot et al., 1996), Fe-bearing Olivine (cyan solid line) (Liu and Li, 2006), pure Opx (magenta solid line) (Zhao et al., 1995; Shinmei et al., 1999), pure Cpx (yellow solid line) (Zhao et al., 1998), and Fe-bearing Cpx (dark yellow solid line) (Nishihara et al., 2003). The PREM density profile is also shown (dashed line). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

sity profile of hydrous pure pyrope was  $\sim 4\%$  higher than the PREM density profile, but closer to the PREM than the anhydrous pure pyrope ( $\sim 5\%$  higher) and Fe-bearing pyrope ( $\sim 6.5\%$  higher) density profile. Furthermore, the density profile of pure olivine and pure Cpx was  $\sim 3\%$  and  $\sim 2\%$  lower than the PREM density profile, respectively, whereas the density profiles of Fe-bearing olivine and Fe-bearing Cpx were very close to the PREM density profile. In conclusion, the density profiles of the upper mantle minerals at the relevant P-T conditions are highly dependent on their iron content. Based on the phase diagram of Opx (Woodland, 1998), we assume that the Opx phase (*Pbca*) transitions into the HP-Cpx phase (*C2/c*) at 250 km ( $\sim 8$  GPa) and is accompanied by a density jump, where the density profile of pure Opx is  $\sim 1.5\%$  lower than the PREM density profile at depths up to 250 km, whereas the density profile of pure Opx is  $\sim 1.5\%$  higher than the PREM density profile at depths under 250 km.

To understand the density profiles and mineralogical models of the upper mantle better, we also modeled the density profiles of the representative upper-mantle mineral assemblages-pyrolyte, using the updated thermoelastic properties of hydrous pyrope for the Earth's upper mantle region between 200 and 400 km depth (Fig. 10). The pyrolyte model represents the global mineral compositions of the upper mantle that are commonly used for comparison between mineral physics results and global density profiles (Lu et al., 2013). The mineral assemblage in pyrolyte model includes  $\sim 63\%$  olivine,  $\sim 15\%$  garnet,  $\sim 16\%$  clinopyroxene, and  $\sim 6\%$  orthopyroxene (Ita and Stixrude, 1992). Here, we made two assumptions: first, the chemical compositions of the constituent minerals do not change in this P-T range, which results in constant zero-pressure densities of the constituent minerals; and second, the volume proportions of the constituent minerals of pyrolyte model are constant. The results are shown in Fig. 10, and the PREM density profile is also shown in this figure for comparison. Fig. 10 shows the density profiles of pyrolyte with hydrous pyrope and other pure minerals, and pyrolyte with anhydrous pyrope and other pure minerals at Earth's upper mantle region between a 200 and 400 km depth. The density profile of pyrolyte with hydrous pyrope and other pure minerals is slightly lower than pyrolyte with anhydrous pyrope and other pure minerals, which show that hydrogen in pyrope can decrease the density of the pyrolyte model. However, according to the "pyrolyte" model, the chemistry of the upper mantle minerals should contain certain components of Fe (Ringwood, 1975). Thus, Fig. 10 also shows that the pyrolyte model with all Fe-bearing minerals and the pyrolyte model with hydrous pyrope and other Fe-bearing minerals, using the Fe-bearing minerals from Fig. 9. From Fig. 10, the pyrolyte model with all Fe-bearing minerals shows the largest density profile; whereas using the hydrous pyrope instead of the anhydrous Fe-bearing pyrope meant the modeled pyrolyte with hydrous pyrope and other Fe-bearing minerals showed a lower density profile than the pyrolyte model with all Fe-bearing minerals towards the PREM density profile (Fig. 10). Furthermore, considering that the volume proportion of pyrope in the pyrolyte model is relatively small compared with olivine and pyroxene, incorporating water into the olivine and pyroxene of the upper mantle may make the density profiles of the pyrolyte model match the PREM density profile well. This once again



**Fig. 10.** Calculated density profiles of the pyrolyte model. In these calculations, the zero-pressure densities and mineral proportions of the constituent minerals are assumed to be constant. The PREM density profile is also shown (dashed line).

proves that the nominally anhydrous mineral phases in the Earth's upper mantle (olivine, pyroxene, and garnet) can contain a significant amount of hydrogen. However, this still needs to be confirmed by measuring the thermoelasticity of all major hydrous upper mantle minerals (Fe-bearing) at relevant P-T conditions in future experiments.

## 5. Conclusions

Incorporating 900 ppmw of water in pyrope crystal yields a reduction in its bulk modulus of 7%, a slight increase in its bulk modulus pressure derivative and thermal expansion coefficient, but little change in its bulk modulus temperature derivative. The presence of water in pyrope helps to reduce the densities of the pyrolite model to better match the density profile of the PREM. Incorporating water in olivine and pyroxene is favorable for reconciling the discrepancy in the density profiles between the mineral physics models and the seismological model (PREM).

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