

RESEARCH ARTICLE

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Key Points:

- We build an integrated thermodynamic model of Fe and Al chemistry for lower mantle conditions
- We find a new stratified picture of the Fe speciation profile with respect to pressures
- The Fe partitioning between ferropericlasite and bridgmanite is dominated by Fe^{2+} spin transition

Supporting Information:

- Supporting Information S1

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Iron partitioning between ferropericlasite and bridgmanite in the Earth's lower mantle

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Abstract Earth's lower mantle is generally believed to be seismically and chemically homogeneous because most of the key seismic parameters can be explained using a simplified mineralogical model at expected pressure-temperature conditions. However, recent high-resolution tomographic images have revealed seismic and chemical stratification in the middle-to-lower parts of the lower mantle. Thus far, the mechanism for the compositional stratification and seismic inhomogeneity, especially their relationship with the speciation of iron in the lower mantle, remains poorly understood. We have built a complete and integrated thermodynamic model of iron and aluminum chemistry for lower mantle conditions and from this model has emerged a stratified picture of the valence, spin, and composition profile in the lower mantle. Within this picture the lower mantle has an upper region with Fe^{3+} -enriched bridgmanite with high-spin ferropericlasite and metallic Fe and a lower region with low-spin, iron-enriched ferropericlasite coexisting with iron-depleted bridgmanite and almost no metallic Fe. The transition between the regions occurs at a depth of around 1600 km and is driven by the spin transition in ferropericlasite, which significantly changes the iron partitioning and speciation to one that favors Fe^{2+} in ferropericlasite and suppresses Fe^{3+} and metallic iron formation. These changes lead to lowered bulk sound velocity by 3–4% around the middle-lower mantle and enhanced density by ~1% toward the lowermost mantle. The predicted chemically and seismically stratified lower mantle differs dramatically from the traditional homogeneous model.

1. Introduction

Recent mineral physics studies have revealed the complex nature of the spin and valence states of iron in ferropericlasite (Fp) and bridgmanite (Pv) at high pressure and temperature (P - T). The spin crossover of Fe^{2+} in Fp occurs over a wide P - T range corresponding to approximately 1100 km to 1900 km in depth [Badro *et al.*, 2003; Goncharov *et al.*, 2006; Lin *et al.*, 2005; Persson *et al.*, 2006; Sturhahn *et al.*, 2005; Tsuchiya *et al.*, 2006; Vilella *et al.*, 2015], whereas the Fe^{3+} in the octahedral site (B site) of Pv undergoes the transition from about 1000 km to 1500 km in depth [Catalli *et al.*, 2011a; Hsu *et al.*, 2011, 2012], both depending somewhat on temperature. Of particular interest to our understanding of deep-mantle seismology are the effects of the spin transition on the density and sound velocity profiles in lower mantle Fp [Cammarano *et al.*, 2010; Crowhurst *et al.*, 2008; Marquardt *et al.*, 2009; Wu and Wentzcovitch, 2014], where abnormal velocity softening within the transition has been reported and the full low-spin state has been found to exhibit distinct elastic behaviors from its full high-spin counterpart. Also of interest is the variation of Fe valence states (Fe^{2+} , Fe^{3+} , and Fe^0) with respect to depth because this variation determines both the amount of Fe that undergoes each type of spin transition and the amount of metallic Fe (Fe^0), which has a significant influence on our understanding of the partial melting in the mantle [Fukai and Suzuki, 1986] and the Earth's core formation [Halliday and Lee, 1999]. In addition, the Fe partitioning between Pv and Fp ($K_D^{\text{Pv-Fp}} = (\text{Fe}/\text{Mg})_{\text{Pv}}/(\text{Fe}/\text{Mg})_{\text{Fp}}$) is also critical to the interpretation of the deep-Earth geochemistry, because changes in partitioning can lead to a chemically stratified lower mantle that may behave distinctly from a traditional homogeneous model. While all these separate aspects of spin, valence, and partitioning are important, their impact on the lower mantle can only be properly determined when their couplings are taken into account through an integrated picture of Fe chemistry under lower mantle conditions. The Fe chemistry is expected to couple to multiple interacting aspects of the lower mantle environment, including P - T , spin transitions, oxygen fugacity, and aluminum substitution. Understanding and quantifying such couplings requires an integrated thermodynamic model of Fe chemistry that incorporates all of these environmental factors.

Using a pyrolitic composition, iron has been shown experimentally to partition into Pv and Fp with a $K_D^{\text{Pv-Fp}} \approx 0.5$ ($K_D^{\text{Pv-Fp}}$ is defined as $[\text{Fe}^{2+} + \text{Fe}^{3+}]_{\text{Pv}} / ([\text{Mg}^{2+}]_{\text{Pv}}) / ([\text{Fe}^{2+}]_{\text{Fp}} / [\text{Mg}^{2+}]_{\text{Fp}})$) [Irifune *et al.*, 2010; Nakajima *et al.*, 2012]. However, $K_D^{\text{Pv-Fp}}$ was observed to significantly increase to almost 0.9 at approximately 28 GPa (or ~750 km depth) [Irifune *et al.*, 2010]. The change in $K_D^{\text{Pv-Fp}}$ has been attributed to the formation of Fe^{3+} -rich Pv promoted by the charge-coupled substitution of Al^{3+} and Fe^{3+} [Frost *et al.*, 2004; Irifune *et al.*, 2010]. On the other hand, self-disproportionation of Fe^{2+} into Fe^0 and Fe^{3+} has also been used to explain the observations of the high Fe^{3+} content in Pv and the coexistence of metallic iron [Frost *et al.*, 2004]. At P - T conditions below the middle-lower mantle, experimental studies have also shown that $K_D^{\text{Pv-Fp}}$ decreases to approximately 0.5 in the pyrolitic composition or to 0.2 in the olivine composition [Auzende *et al.*, 2008; Irifune, 1994; Irifune *et al.*, 2010; Kesson *et al.*, 1998; Kobayashi *et al.*, 2005; Sakai *et al.*, 2009; Sinmyo *et al.*, 2008a; Wood, 2000]. A recent theoretical work of Muir and Brodholt [2016] studied the ferrous iron partitioning between Pv and Fp and predicted that Fe^{2+} prefers Fp rather than Pv. Their calculations showed a convex shape feature of the $K_D^{\text{Pv-Fp}}(P)$ profile with a peak ($K_D^{\text{Pv-Fp}} \sim 0.25$) at 50 GPa and gradually decreasing to 0.05 at higher pressures. However, they only calculated the ferrous iron Fe^{2+} partitioning in the two phases, which is $(\text{Mg}_{1-x}\text{Fe}^{2+}_x)\text{O} + \text{MgSiO}_3 \rightleftharpoons (\text{Mg}_{1-y}\text{Fe}^{2+}_y)\text{SiO}_3 + \text{MgO}$. The important impurity species Al^{3+} and Fe^{3+} in the Pv phase, the possible formation of metallic Fe phase, and the influence of the surrounding oxygen fugacity ($f\text{O}_2$) conditions are not considered in their thermodynamic model. Thus far, the relationship of Fe partitioning with Fe valence and spin states at lower mantle relevant P - T , composition (X), and $f\text{O}_2$ conditions remain largely unexplored. Here we have developed an integrated and validated ab initio and empirical fitting-based thermodynamic model to explicitly predict the partitioning behavior of Fe in lower mantle Pv and Fp over a wide range of likely P - T - X - $f\text{O}_2$ conditions in pyrolite and olivine compositional models. We have used density functional theory (DFT) calculations with the HSE06 hybrid exchange-correlation functional [Heyd *et al.*, 2003] for the relevant enthalpies. The equilibrium iron valence, spin states, and occupation in the sublattices of Fp and Pv are determined by minimizing the total Gibbs free energy of the system (section 4.2 for details). Since it is well known that the variation in the oxygen fugacity ($f\text{O}_2$) affects Fe valence states in the upper mantle minerals, it is important to consider its possible impact on the lower mantle bridgmanite, and therefore, here we have considered two different scenarios in our modeling: a closed system with no exchange of free oxygen with surrounding materials where Fe^{3+} is produced through the charge disproportionation (chg. disp.) reaction ($3\text{Fe}^{2+} \rightarrow 2\text{Fe}^{3+} + \text{Fe}^0$) [Frost *et al.*, 2004; Xu *et al.*, 2015; Zhang and Oganov, 2006] and an open system with free oxygen buffered through oxygen exchange with surrounding materials in the system (section 4.2 for details). These modeling approaches allow us to investigate the iron chemistry under lower mantle conditions (closed system scenario) and to compare with experimental observations where the $f\text{O}_2$ is usually buffered by certain capsules (open system scenario), typically resulting in relatively oxidizing conditions compared to the lower mantle [Irifune *et al.*, 2010]. The effects of Al^{3+} incorporation are investigated via the integration of the Al^{3+} substitution energetics in the pyrolite system, and comparison with the olivine system yields understanding of the discrepancy between Al-bearing and Al-free systems of the reported K_D values in previous experimental reports [Auzende *et al.*, 2008; Irifune, 1994; Irifune *et al.*, 2010; Kesson *et al.*, 1998; Kobayashi *et al.*, 2005; Sakai *et al.*, 2009; Sinmyo *et al.*, 2008a; Wood, 2000].

2. Results and Discussion

Our ab initio and empirical fitting-based thermodynamic model predicts that a gradual spin transition occurs for Fe^{2+} in Fp from approximately 40 GPa to 80 GPa and for B-site Fe^{3+} in Pv from approximately 30 GPa to 50 GPa (Figure 1a), both of which are along an expected geotherm [Brown and Shankland, 1981]. The predicted fractions of different Fe species in the pyrolitic compositional system show that high-spin Fe^{2+} is the predominant form of Fe in Fp and Pv around the top of the lower mantle and it should be noted that Fe^{3+} is produced only through the chg. disp. reaction in Pv. Our model predicts the formation of metallic Fe from the top to the middle-lower mantle. Once sufficient Al^{3+} is dissolved into Pv, most B-site Fe^{3+} is driven to the A-site (Figure 1b) (details of the Al content in Pv are discussed in section 4.1, and the driving force for A-site occupancy is discussed in supporting information (SI) section 2). The loss of B-site Fe^{3+} implies that the spin transition of Pv B-site Fe^{3+} will not have a significant impact on the physical and chemical properties of the lower mantle [Hsu *et al.*, 2012]. Furthermore, Fe^{2+} preferentially partitions into Fp across its spin transition such that Pv is depleted of iron toward the lowermost mantle. This spin-induced iron partitioning

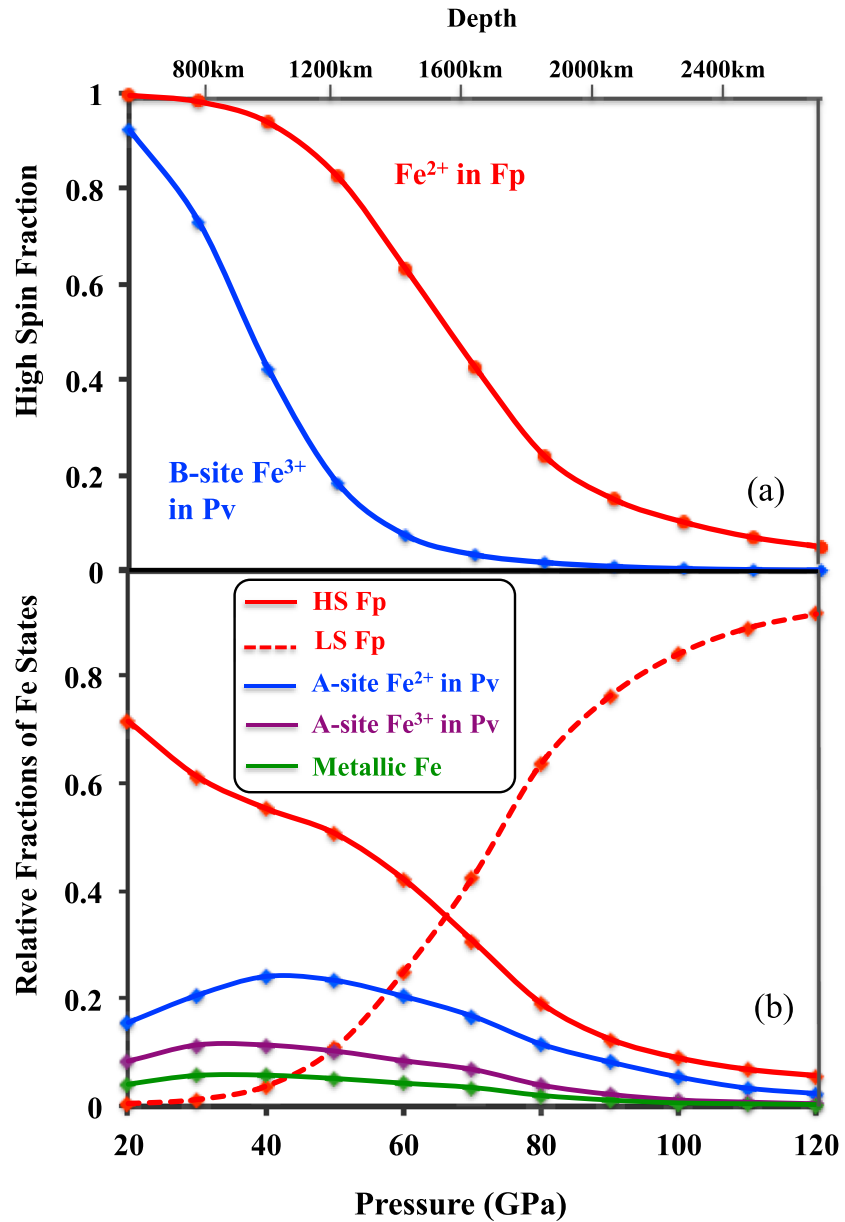


Figure 1. Spin and valence states of iron and their relative fractions in the lower mantle ferropericlase (Fp) and bridgmanite (Pv) along an expected geotherm [Brown and Shankland, 1981]. Solid symbols represent our theoretically predicted results, while colored lines are fitted to the data to show trends. (a) Fractions of the high-spin Fe^{2+} in Fp and high-spin B-site Fe^{3+} in Pv are plotted as red and blue lines, respectively. (b) Relative fractions of iron in lower mantle Fp, Pv, and metallic iron with respect to the total amount of Fe in a pyrolitic compositional model. The B-site Fe^{3+} content in Pv is significantly smaller ($\leq 10^{-6}$ mol fraction of Fe) than the contents of other Fe species and is not shown for clarity.

suppresses the aforementioned chg. disp. reaction, significantly decreasing the presence of the metallic iron in the lower parts of the lower mantle. Therefore, the formation of metallic Fe is predicted to occur only from the top to the middle-lower mantle.

The partitioning coefficient ($K_D^{\text{Pv-Fp}}$) is calculated using the predicted iron contents in Fp and Pv for expected geotherm P - T conditions of the pyrolitic lower mantle (Figure 2a, and $\ln(K_D^{\text{Pv-Fp}})$ is given in SI Figure S6). Our predicted K_D curve shows a convex shape starting with an initial value of 0.2 at 22 GPa, a peak value of 0.34 at 40 GPa, and a continuous decrease between 40 GPa and 120 GPa reaching a minimum value of almost zero. At the topmost lower mantle, Fe^{2+} is more energetically favorable to partition into Fp. As the P - T increases up

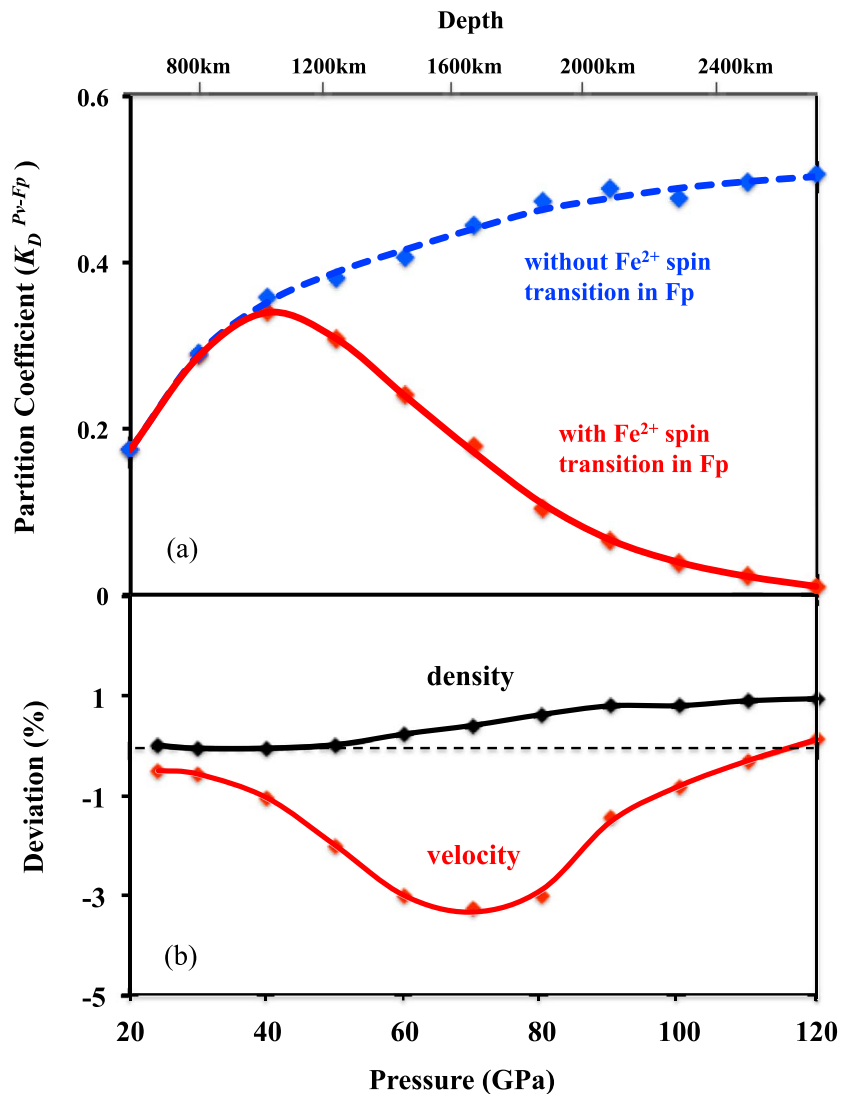


Figure 2. Partition coefficient (K_D^{Pv-Fp}) of iron and deviations in the density and bulk sound velocity due to the Fp Fe^{2+} spin transition in a pyrolytic lower mantle composition along an expected geotherm [Brown and Shankland, 1981]. (a) Red data points with fitted solid curve are the K_D considering the spin transition Fe^{2+} in Fp. Blue data points with fitted dashed line curve are the K_D without the influence of this spin transition; K_D values continue to increase with increasing pressure along the geotherm. (b) The deviation is defined as $(X' - X_{ref})/X_{ref}$, where X' is the physical property (density (ρ) or bulk sound velocity (V_ϕ)) calculated using a pyrolytic model across the Fe spin transition along an expected geotherm [Brown and Shankland, 1981], X_{ref} is the reference value without the spin transition. Black and red data points and fitted solid curves correspond to the density and bulk sound velocity deviations (%), respectively, from the reference profiles without the spin transition of Fe^{2+} in Fp.

to 40 GPa, the incorporation of Al^{3+} into Pv through the dissolution of majorite drives both high-spin Fe^{2+} and Fe^{3+} into the A-site of the Pv lattice. Another reason causing more iron partitioning into Pv from 20 to 40 GPa is that the majority of Fp Fe^{2+} is in the high-spin state, where its enthalpy becomes relatively higher as pressure increases as compared to Pv Fe^{2+} (see SI section 2.3 for detailed discussion). Compared with the K_D curve without the spin transition in Fp that continuously increases with increasing pressure (Figure 2a), it is evident that the dramatic decrease in the K_D curve starting at approximately 40 GPa is caused by the spin transition in Fp. The volume collapse and the associated reduction in the Gibbs free energy make the low-spin Fe^{2+} with a smaller volume more energetically favorable in Fp, as opposed to staying in Pv. As the spin crossover continues to occur with increasing depth, the K_D value below the spin transition zone reaches almost zero, and the majority of the iron partitions into Fp at the lowermost mantle. This

partitioning also destabilizes metallic iron in the system, reducing it to less than 1% of the Fe toward the deeper lower mantle. The Fp Fe^{2+} spin transition governing Fe partitioning profile shown in our calculation matches very well with the results in the recent theoretical work of *Muir and Brodholt* [2016]. The same convex shape feature of the Fe partitioning coefficient with respect to pressures was reported in their work [*Muir and Brodholt*, 2016, Figure 7]. The peak position was 50 GPa in their calculation, very close to the 40 GPa peak position in our results (Figure 2a). For the quantitative comparison, the peak value of Fe partitioning coefficient was about 0.25 in their results, while we find a peak value about 0.35 in our calculation. This small quantitative difference may come from the fact that Muir and Brodholt did not include the Fe^{3+} and Al^{3+} in the Pv phase in their model. As the existence of Fe^{3+} and Al^{3+} increases the Fe content in the Pv phase, their inclusion in our model is expected to yield a relatively higher Fe partitioning coefficient $K_D^{\text{Pv-Fp}}$. In addition, Muir and Brodholt based their DFT calculations on the generalized gradient approximation with the Hubbard U corrections (GGA + U) while we used the HSE06 hybrid functional in our work, which is generally believed to be a more consistent and accurate method. However, our results are consistent with their findings both qualitatively and quantitatively, lending support to both models.

To understand the consequences of Fp Fe^{2+} spin transition and Fe partitioning on the seismic profiles of the Earth's lower mantle, we have also modeled the mass density (ρ) and bulk sound velocity (V_ϕ) profiles of a representative pyrolitic lower mantle composition along an expected mantle geotherm [*Brown and Shankland*, 1981] (calculation details are shown in SI section 4.2 [*Tange et al.*, 2012, 2009; *Dubrovinsky et al.*, 2000; *Lu et al.*, 2013; *Murakami et al.*, 2012; *Ricolleau et al.*, 2010; *Shukla et al.*, 2015; *van Westrenen et al.*, 2005; *Wang et al.*, 2015; *Wu and Wentzcovitch*, 2014]) and compared them with the density and bulk velocity without the Fe^{2+} spin transition in Fp (Figure 2b). Here the bulk sound velocity is defined as $V_\phi = (K_S/\rho)^{1/2}$, where K_S is the adiabatic bulk modulus and values are taken along the geotherm. We only include Pv, Fp, and metallic Fe in our model as they occupy more than 90% of the volume of the lower mantle (SI section 4.2). The starting zero-pressure relative volumetric ratio of Pv over Fp in our pyrolitic model is $V(\text{Al, Fe-bearing Pv}):V(\text{Fp}) = 3.5:1$ [*Irifune et al.*, 2010]. Our calculated density and velocity profiles display continuous increase with increasing depth without any abrupt changes. However, compared with the calculated profiles without the spin transition, we do notice lowered bulk sound velocity around middle-lower mantle by 3–4% and enhanced density by 1% toward the bottom of the lower mantle. These changes can be explained by the spin transition of Fe^{2+} in Fp. As the low-spin Fe^{2+} in Fp has a relatively smaller volume than its high-spin counterpart, the volume of Fp will decrease when the spin transition occurs, increasing the density of the system near the bottom of the lower mantle. This volume collapse also causes a softened bulk modulus in the spin transition region (40–80 GPa) leading to a lowered bulk sound velocity ($V_\phi = (K_S/\rho)^{1/2}$) for the system due to the spin transition. The predicted profiles also show a lowered bulk sound velocity by up to 2% with respect to the preliminary reference Earth model (see SI section 3.4 [*Dziewonski and Anderson*, 1981]).

Comparison of our theoretical predictions in the oxidation reaction model at experimental P - T - $f\text{O}_2$ conditions with previous experimental results [*Auzende et al.*, 2008; *Irifune*, 1994; *Irifune et al.*, 2010; *Kesson et al.*, 1998; *Kobayashi et al.*, 2005; *Sakai et al.*, 2009; *Sinmyo et al.*, 2008a; *Wood*, 2000] for the iron partitioning shows distinctions between the pyrolite composition containing Al^{3+} and the olivine bulk composition without Al^{3+} . We use a representative $f\text{O}_2$ range of $\log f\text{O}_2[\text{diamond-carbonate}] \leq \log f\text{O}_2 \leq \log f\text{O}_2[\text{diamond-carbonate}] + 2$, as discussed in SI section 3.2 [*Irifune et al.*, 2010; *Pownceby and O'Neil*, 1994; *Stagno and Frost*, 2010; *Stagno et al.*, 2015]. Here the symbol $f\text{O}_2[X]$ represents the fugacity of material X under the given P - T conditions. For the notation of $f\text{O}_2[\text{diamond-carbonate}]$, diamond-carbonate represents the equilibrium described by the reaction $\text{C (diamond)} + \text{O}^{2-} (\text{mineral/melt}) + \text{O}_2 \rightleftharpoons \text{CO}_3^{2-} (\text{mineral/melt})$ [*Stagno and Frost*, 2010]. The equilibrium of carbon (diamond) coexisting with carbonates happens in the (lower mantle relevant) high-pressure condition. The above reaction sets the $f\text{O}_2$ of the diamond capsule. We assume that within the lower mantle relevant P - T of our thermodynamic model, the $f\text{O}_2[\text{diamond-carbonate}]$ is always 4 orders of magnitude lower than the Re-ReO₂ capsule $f\text{O}_2$ [*Nakajima et al.*, 2012; *Pownceby and O'Neil*, 1994; *Stagno and Frost*, 2010; *Xu et al.*, 2015]. The Re-ReO₂ capsule $f\text{O}_2$ values as a function of P - T are explicitly shown in our previous work [*Xu et al.*, 2015]. Although both of the pyrolitic composition curve and the olivine composition curve show convex K_D behavior with respect to depth, the magnitude of the K_D in the olivine model is a smaller by a factor of 3–4 than that in the pyrolite model (Figure 3). Under the $f\text{O}_2$ range studied no chg. disp. occurs and more Fe^{3+} is formed and incorporated into Pv compared to under lower mantle $f\text{O}_2$, leading to

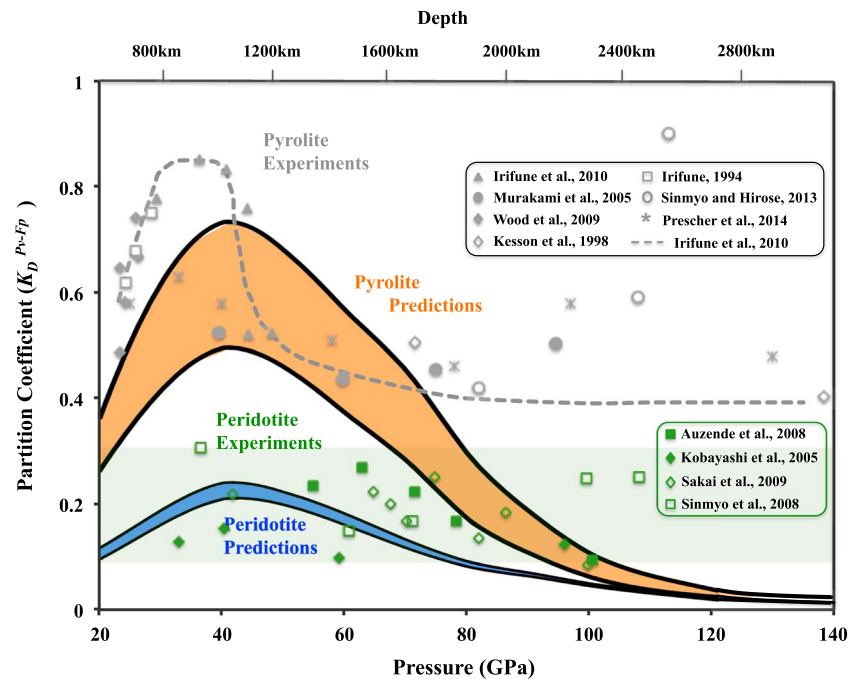


Figure 3. Comparison of the partition coefficient (K_D) of iron between Pv and Fp from experimental and theoretical results. The orange color region represents our theoretical predicted range of K_D in a pyrolite composition model. The lower limit (black line) of the orange region corresponds to the condition that $\log fO_2 = \log fO_2[\text{diamond-carbonate}]$, and the upper limit (black line) corresponds to the condition that $\log fO_2 = \log fO_2[\text{diamond-carbonate}] + 2$. The blue color region represents our predicted K_D range having a bulk composition of olivine (does not contain any Al^{3+}) under the same fO_2 range used in for the pyrolite composition. Experimental K_D values in a pyrolite composition model (grey symbols) [Irifune, 1994; Irifune et al., 2010; Kesson et al., 1998; Murakami et al., 2005; Prescher et al., 2014; Sinmyo and Hirose, 2013; Wood, 2000] (dashed grey curve is obtained from Irifune et al. [2010]) and olivine composition (green symbols) [Auzende et al., 2008; Kobayashi et al., 2005; Sakai et al., 2009; Sinmyo et al., 2008a] are also plotted for comparison.

a higher K_D than the chg. disp. reaction model. The contents of different Fe species (valence and spin states) in the pyrolitic compositional model under the $fO_2[\text{diamond-carbonate}]$ condition are shown in SI section 3.3 Figure S7. This fO_2 effect explains why the pyrolitic K_D profile in Figure 3 (oxidation reaction model) is higher than that in Figure 2a (chg. disp. reaction) and demonstrates the importance of maintaining realistic lower mantle fO_2 when measuring K_D . The difference in the magnitude between the pyrolite and olivine compositional models can be explained by the existence of Al^{3+} , which enhances the Fe^{3+} content in Pv in the pyrolite model due to the formation of the stable $Fe^{3+}-Al^{3+}$ pair. As there is no Al^{3+} in the olivine model, the K_D values are predicted to remain at 0.1–0.2. For the pyrolite composition, the K_D profiles from experiments [Irifune, 1994; Irifune et al., 2010; Kesson et al., 1998; Murakami et al., 2005; Wood, 2000] and our simulations both exhibit a convex shape. However, the experimental results show a sharp decrease at approximately 40 GPa and a flattening K_D value of around 0.5 at higher pressures, which differ from our predicted gradual decrease of K_D (Figures 2a and 3). The gradual decrease in our calculated K_D values is due to the broad spin crossover of Fp Fe^{2+} at high P - T conditions of the lower mantle [Crowhurst et al., 2008; Lin et al., 2005; Tsuchiya et al., 2006]. Future high P - T experimental data with lower uncertainties are needed to explain the discrepancies (see SI section 3.3 for further discussion of the discrepancies [Ammann et al., 2010; Irifune, 1994; Irifune et al., 2010; Murakami et al., 2005; Xu et al., 2015]).

Recent two experimental works about the Fe partitioning behavior in a pyrolitic compositional sample under lower mantle relevant P - T condition showed a large K_D increase at about 100 GPa [Prescher et al., 2014; Sinmyo and Hirose, 2013]. The explanation proposed in the work [Prescher et al., 2014] for the K_D increase is that the Fe^{2+} undergoes a spin transition from the intermediate spin (IS) to the low-spin state in Pv, which is inconsistent with the widely held belief that Fe^{2+} is always in the HS state in Pv throughout the lower mantle pressure range [Bengtson et al., 2008; Grocholski et al., 2009; Hsu et al., 2010a; Jackson et al., 2005; Lin et al., 2012;

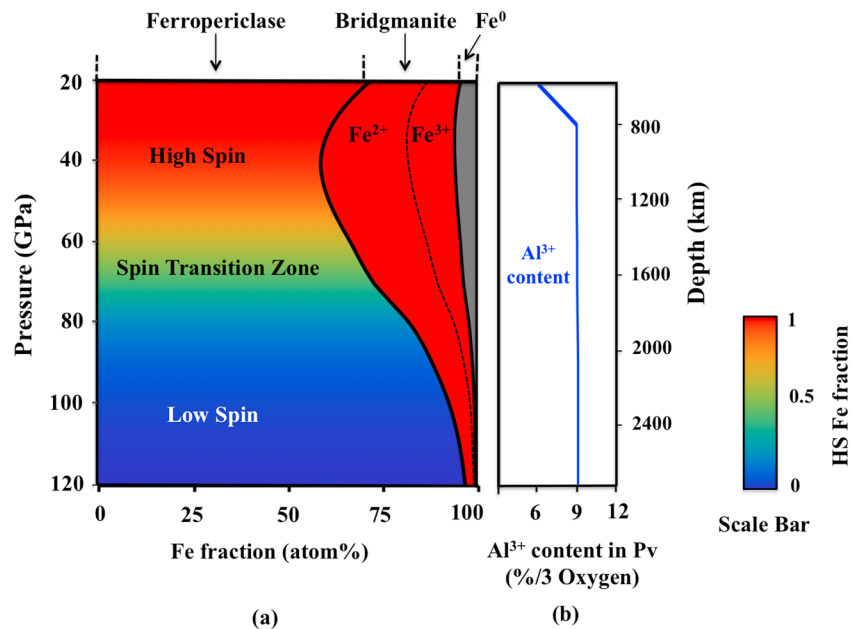


Figure 4. Variations of iron chemistry in a pyrolitic lower mantle model. (a) The fractions of the total amount of Fe in atom % in Fp, Pv, and metallic Fe phase (Fe^0) as a function of depth are represented by different color regions. The color gradient represents the high-spin (HS) fraction of iron in both Fp and Pv phases as shown in the vertical bar on the right. In the Pv region, the dashed line separates the A-site Fe^{3+} fraction and A-site Fe^{2+} fraction in Pv. (b) The Al content in Pv (per three oxygen atoms) is shown by the blue solid line.

Stackhouse *et al.*, 2007]. Moreover, even if we assume that this spin transition occurs, the same K_D increase behavior would then be expected to happen for the Al-free case as well. However, many previous experimental works failed to observe this abnormally high K_D around 100 GPa [Auzende *et al.*, 2008; Nakajima *et al.*, 2012; Sakai *et al.*, 2009]. The explanation for this K_D increase proposed in the work [Sinmyo and Hirose, 2013] is the B-site Fe^{3+} spin transition in Pv. However, we would argue that this is unlikely to be the mechanism causing the K_D increase, because the population of Fe^{3+} in B-site in the Al-bearing Pv is very small [Hsu *et al.*, 2012; Zhang and Oganov, 2006] (also discussed in SI section 2.1 in our work) and this spin transition region reported in many previous works is from the upper to the middle-lower mantle [Catalli *et al.*, 2010; Hsu *et al.*, 2011; Lin *et al.*, 2012; Xu *et al.*, 2015]. Specifically, the experimental work of Lin *et al.* [2012] reported that the B-site Fe^{3+} spin transition is at about 25 GPa based on their quadrupole splitting (QS) measurement. The simulation work of Hsu *et al.* [2011] predicted that the gradual B-site Fe^{3+} spin transition is from 40 GPa to 70 GPa at $T=2000$ K. So it is less likely for this B-site Fe^{3+} spin transition to have such a significant impact on Fe partitioning above 100 GPa. Moreover, some previous experimental works also showed that there is no K_D increase around or above 100 GPa [Irifune *et al.*, 2010; Kesson *et al.*, 1998]. Even in the paper Prescher *et al.* [2014], they showed that K_D drops back to 0.5 at about 130 GPa. If this abnormal K_D increase is indeed caused by the B-site Fe^{3+} spin transition, K_D would stay at the high value down to the bottom of the lower mantle, which is inconsistent with the observation of Prescher *et al.* [2014]. We also note that the explanations for the abnormal K_D increase in the experimental works Prescher *et al.* [2014] and Sinmyo and Hirose [2013] are inconsistent with each other. Overall, the collected experimental results and efforts to explain them show that there is still significant uncertainty for the experimental K_D at high pressure (>100 GPa). More work is needed to robustly determine K_D under these extreme conditions.

3. Conclusions

Our calculations have demonstrated that the Earth's lower mantle can be separated into distinct layers that are controlled by the spin crossover in Fp and the Al^{3+} substitution in Pv (summarized in Figure 4). The top layer is characterized by Fe^{3+} -enriched Pv coexisting with high-spin Fp and metallic iron, while the bottom

layer at depths approximately below about 2000 km exhibits Fe predominantly in Fp and almost no metallic Fe. The transition between the two layers occurs through the Fp Fe^{2+} spin transition zone (Figure 4). The volume collapse of Fp caused by the spin crossover also leads to a lowered bulk sound velocity around the middle-lower mantle (Figure 2b). These changes suggest that there is significant iron chemistry-induced stratification of the lower mantle, in contrast to the traditional view of chemical and seismic homogeneity in the lower mantle.

4. Methods

4.1. Composition Models of Our Thermodynamic System

4.1.1. Pyrolitic Lower Mantle Composition

The Earth's lower mantle is proposed to consist of pyrolite which contains approximately one third basalt and two third peridotite [Ringwood, 1966]. In the pyrolitic compositional model, the mineralogy of the lower mantle is mainly made of approximately 70% bridgmanite ((Mg,Fe)(Si,Al) O_3 ; Pv), 20% ferropericlase ((Mg,Fe)O; Fp), and 10% calcium silicate perovskite (CaSiO_3 ; Ca-Pv) [Irifune *et al.*, 2010], where all percentages are by volume. Since Ca-Pv likely does not incorporate significant Fe in its lattice, we have only considered Pv and Fp phases in the lower mantle system with a molar ratio [(Mg,Fe)(Si,Al) O_3]: [(Mg,Fe)O] = 1: 0.65 corresponding to the volumetric ratio $V[(\text{Mg,Fe})(\text{Si,Al})\text{O}_3]: V[(\text{Mg,Fe})\text{O}] = 3.5: 1$. The Al^{3+} cation is considered to be mainly incorporated into Pv in the lower mantle. Previous studies have shown that the Al^{3+} content in Pv increases with increasing depth at the topmost lower mantle as a result of majorite dissolution into Pv [Irifune, 1994; Irifune *et al.*, 2010]. The depth-dependent Al^{3+} content in Pv has been considered in our calculations in order to understand its incorporation mechanism and effects on the iron partitioning between Pv and Fp phases. As the starting composition of the pyrolite system in our calculations, Al^{3+} content in Pv increases from 0.06 to 0.09 per three oxygen atoms from 20 GPa to 30 GPa and stays at 0.09 per three oxygen atoms from 30 GPa to 120 GPa, and Fe content is 0.1 per three oxygen atoms in Pv and 0.12 per oxygen atom in Fp from 20 GPa to 120 GPa. The values are based on experimental measurements of Al and Fe content from the previous reference [Irifune *et al.*, 2010].

4.1.2. Olivine Compositional Model

In the olivine compositional model we treat the composition as equal to that of olivine. Olivine, the most abundant mineral in the upper mantle, transforms to Pv and Fp in the lower mantle P - T conditions. The Fe partitioning coefficient (K_D) between Pv and Fp phases with a bulk olivine composition in the lower mantle is also considered in our calculations. Since this system contains a negligible amount of Al^{3+} , it is also used to understand how the substitution of Al^{3+} in Pv affects the iron partitioning compared to pyrolitic composition case. The typical Fe content in olivine is about 0.1 Fe per Mg-site [Auzende *et al.*, 2008; Sinmyo *et al.*, 2008b]. For the starting composition of the olivine system in our calculation, we have used San Carlos olivine with a representative chemical formula $(\text{Mg}_{0.9}\text{Fe}_{0.1})_2\text{SiO}_4$.

4.2. Thermodynamic Modeling of the Pv + Fp System

To understand the Fe partitioning the lower mantle under relevant experimental conditions, we have modeled a bulk composition of both pyrolite and olivine, as described in sections 4.1.1 and 4.1.2. In the model, the total amount of iron is fixed throughout all lower mantle conditions. Although the thermodynamic equilibrium state depends on overall stoichiometry and chemical potentials, the equilibrium state is independent of how we approach it. However, for clarity we consider the system to be equilibrating from an initial state with specific spin and site occupancies consistent with the overall stoichiometric constraints. We take our initial state as high-spin (HS) Fe^{2+} in both Pv and Fp, in which the HS Fe^{2+} occupies the A site in Pv and substitutes for the Mg ions in Fp at the relevant P - T of the lower mantle [Bengtson *et al.*, 2008; Grocholski *et al.*, 2009; Zhang and Oganov, 2006]. We also assume that Al^{3+} enters into the Pv lattice through the charge-coupled substitution in which Al^{3+} - Al^{3+} occupy the A site and B site jointly [Brodholt, 2000]. These initial states are allowed to vary in our calculations in order to reach thermodynamic equilibrium, in which variations are considered for Fe HS and LS states, Fe occupancy of A and B sites in Pv, Fe^{2+} , and Fe^{3+} valence states, and partitioning of Fe between Fp and Pv.

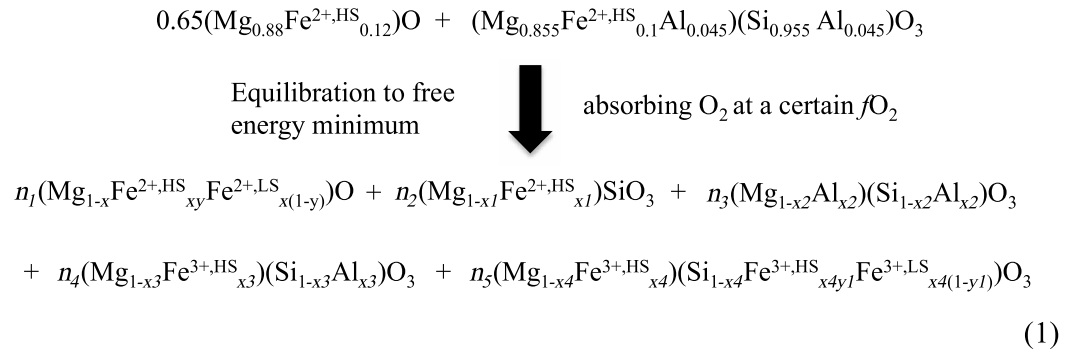
In order to find the final equilibrium state of the system at a given P - T condition, various potential valence and spin states and site occupancies of iron in Pv and Fp phases have been considered in our calculations, as well as two methods of treating the oxygen availability (oxygen fugacity). Specifically, we have considered an

oxidation reaction model (equation (1)) and a chg. disp. reaction model (equation (2)) in our thermodynamic modeling. Variations in the oxygen fugacity (fO_2) are also considered in the oxidation reaction model. Consideration of these different reactions helps us to understand both laboratory experimental results and behavior in the deep mantle, which can have significantly different fO_2 values.

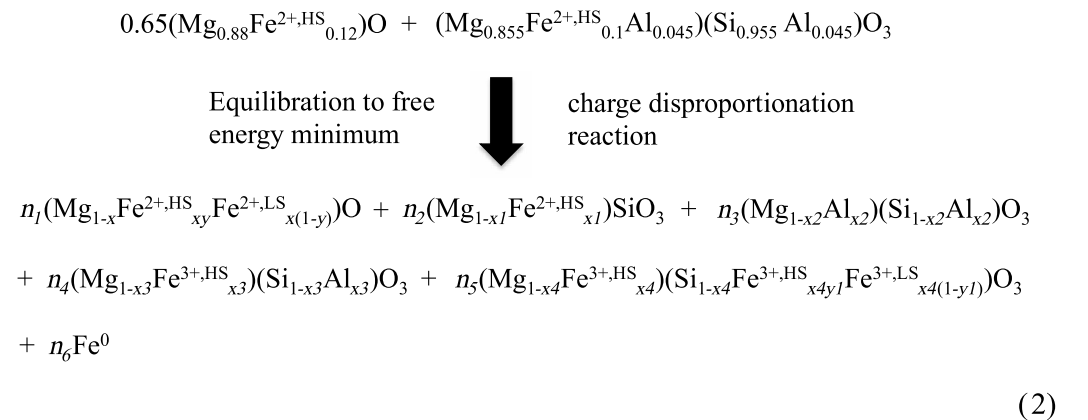
The oxidation reaction model is appropriate for modeling laboratory experiments. In the laboratory, the data were typically derived from chemical analyses of quenched samples originally equilibrated at high temperatures in systems with capsules that effectively buffer the fO_2 . Depending on the type of the capsule used (e.g., metal, MgO, and diamond) and potentially the kinetics in the experiment, the fO_2 of the system can vary significantly, making the interpretation of experimental results more difficult [Campbell *et al.*, 2009; Frost *et al.*, 2004; Irifune *et al.*, 2010; Lauterbach *et al.*, 2000; Nakajima *et al.*, 2012; Xu *et al.*, 2015]. Under equilibrium with the fO_2 set by capsules used in most experimental conditions, metallic Fe cannot form, as it will be oxidized, and there is excess oxygen available to oxidize Fe^{2+} to Fe^{3+} [Xu *et al.*, 2015]. This explains why we do not have metallic Fe (Fe^0) in the oxidation model as shown in the equation (1). In contrast, it is believed that there is no excess oxygen available in the lower mantle, and any Fe^{3+} that forms is created by the chg. disp. reaction ($3Fe^{2+} \rightarrow 2Fe^{3+} + Fe^0$) [Frost *et al.*, 2004; McCammon, 1997; Xu *et al.*, 2015].

The chg. disp. reaction model is appropriate for modeling lower mantle relevant conditions. In this model, we have assumed that the lower mantle is not chemically reacting with the surrounding layers of the upper mantle and the outer core such that there is neither external free oxygen gas nor any significant amount of other oxidizing agents to oxidize Fe^{2+} available. In such a scenario, the only possible mechanism to produce Fe^{3+} is via the chg. disp. reaction.

In the oxidation reaction modeling we consider the following equilibration from our initial state.



In the chg. disp. reaction modeling we consider the following equilibration from our initial state.



For the oxidation reaction model, the grand potential of the system is minimized as a function of P , T , and the chemical potential of oxygen $\mu(O_2)$ such that the system is open to free O_2 . For the charge disproportionation reaction model, the Gibbs energy is minimized as a function of P - T such that the system is closed with respect to oxygen composition.

Equations (3) and (4) detail the phases and sublattice mixtures in a compact form for both models, while equations (5) and (6) express the total thermodynamic potentials of the system. Equation (5) represents the expression of the grand potential, which is minimized for the oxidation reaction model, where Δn is the amount of the absorbed O_2 . This expression makes use of the expression for the grand potential (Ω) as $\Omega = G(Pv + Fp) - \Delta n \times \mu(O_2)$ where $G(Pv + Fp)$ is the total Gibbs energy of the solid phases, Pv and Fp. Equation (S6) is the expression of the Gibbs energy, which is minimized for the chg. disp. reaction model.

We use an ideal solution model to formulate the Gibbs and grand potential energies in equations (5) and (6), which treats the Mg^{2+} , Si^{4+} , Al^{3+} , $(Fe^{2+,HS})_{Fp}$, $(Fe^{2+,LS})_{Fp}$, $(Fe^{2+,HS})_{Pv}$, $(Fe^{3+,HS,A-site})_{Pv}$, $(Fe^{3+,HS,B-site})_{Pv}$, and $(Fe^{3+,LS,B-site})_{Pv}$ species as noninteracting species on each relevant sublattice. We have also checked the nonideality effect and find that it does not have any qualitative impact on the result of our ideal solution model (the details are discussed in SI section 1.2 [Blum and Zunger, 2004]). If one considers these effects, quantitative changes are <0.09 for the Fe partitioning coefficient and <0.01 for the $Fe^{3+}/\Sigma Fe$ in Pv (the relative content of Fe^{3+} in Pv) at all the lower mantle relevant P - T conditions. There is also no change for the Pv B-site occupancy. We thus did not consider the nonideality effect further in our model. In the ideal solution approximation, the mixture enthalpies (H) can be written as a linear combination of their end-member values. The enthalpy of the end-members in the system was obtained DFT calculations. The configurational entropy (S_{config}) and electronic-magnetic entropy of different Fe states (S_{mag}) are modeled in the ideal noninteracting system following the approaches in Tsuchiya *et al.* [2006] and Xu *et al.* [2015]. The only additional terms required in the present model versus the previous reference [Xu *et al.*, 2015] are those in the configurational entropy for systems containing Al. These are treated in the standard way for a multicomponent ideal solution sublattice [Chang and Oates, 2009], e.g., as illustrated in equation (7) for the configurational entropy $S_{config}(Pv, B-site)$ of the B-sublattice in Pv.

With the exception of a special situation for oxygen described next, no vibrational contributions to the free energies are included, as they are assumed to vary slightly between the different possible solid states of the system. The calculation of the vibrational effect is shown in SI section 1.3 [Anderson, 1989; Hsu *et al.*, 2010b; Sha and Cohen, 2010]. Similar to the nonideality effect, the inclusion of the vibrational effect does not have a significantly qualitative impact on our results. The quantitative changes are <0.1 for the Fe partitioning coefficient and <0.05 for the $Fe^{3+}/\Sigma Fe$ in Pv at all the lower mantle relevant P - T conditions. There is also no observable change for the Pv B-site occupancy. Therefore, the vibrational effect is not further considered in our model. The one exception to this approach is in the oxidation reaction model, where O_2 can be absorbed into the system from the gas phase. In this case the vibrational contributions of oxygen atoms are present in the gas phase model and therefore should not be ignored in the ionic solid phase. Therefore, in our thermodynamic model we include an approximate solid phase vibrational free energy for oxygen, which is described in SI section 4.1 [Lee *et al.*, 2009; Yagi *et al.*, 1978].

The fO_2 in different capsules as a function of P - T and the calculation of the effective chemical potential of O_2 can be found in the work of Xu *et al.* [2015] (section) 2.1.1 and SI section 1 for details). Using the expressions in S5 and S6 for the thermodynamic potentials of the system, we have then minimized these potentials to reach thermodynamic equilibrium conditions at any given conditions of the possible variables. More specifically, for the chg. disp. model, in order to find stable mineral phases with equilibrium iron content and spin/valence states, the Gibbs energy, $G_{total}[Chg. Disp.]$, is minimized with respect to $(n_1:n_6, x, x_1:x_4, y, y_1)$ at each given P - T condition. A corresponding minimization is also done for $\Omega_{total}[Oxidation]$.

$$\text{System}_{Oxidation} = (n_2 + n_3 + n_4 + n_5) \left(\frac{Mg_{n_2+n_3+n_4+n_5-x_2n_3-x_1n_2-x_3n_4-x_4n_5}}{n_2+n_3+n_4+n_5} Fe^{2+} \frac{x_1n_2}{n_2+n_3+n_4+n_5} Fe^{3+,HS} \frac{x_3n_4+x_4n_5}{n_2+n_3+n_4+n_5} Al^{3+} \frac{x_2n_3}{n_2+n_3+n_4+n_5} \right) \\ \left(\frac{Si_{n_2+n_3+n_4+n_5-x_2n_3-x_3n_4-x_4n_5}}{n_2+n_3+n_4+n_5} Fe^{3+,HS} \frac{x_4n_5y_1}{n_2+n_3+n_4+n_5} Fe^{3+,LS} \frac{x_4n_5(1-y_1)}{n_2+n_3+n_4+n_5} Al^{3+} \frac{x_2n_3+x_3n_4}{n_2+n_3+n_4+n_5} \right) O_3 + n_1 (Mg_{1-x} Fe_{xy}^{2+,HS} Fe_{x(1-y)}^{2+,LS}) O \quad (3)$$

$$\text{System}_{ChgDisp} = \text{System}_{Oxidation} + n_6 Fe^0 \quad (4)$$

$$\Omega_{total}[Oxidation] = \{ G_{total}[ChgDisp] - n_6 H[Fe^0] + n_6 TS(Fe^0) \} - \Delta n \mu(O_2) \quad (5)$$

$$\begin{aligned}
G_{\text{total}}[\text{ChgDisp}] = & n_1 y H[(\text{Mg}_{1-x} \text{Fe}_x^{2+, \text{HS}}) \text{O}] + n_1 (1-y) H[(\text{Mg}_{1-x} \text{Fe}_x^{2+, \text{LS}}) \text{O}] + n_2 H[(\text{Mg}_{1-x_1} \text{Fe}_{x_1}^{2+, \text{HS}}) \text{SiO}_3] \\
& + n_3 H[(\text{Mg}_{1-x_2} \text{Al}_{x_2}^{3+}) (\text{Si}_{1-x_2} \text{Al}_{x_2}^{3+}) \text{O}_3] + n_4 H[(\text{Mg}_{1-x_3} \text{Fe}_{x_3}^{3+, \text{HS}}) (\text{Si}_{1-x_3} \text{Al}_{x_3}^{3+}) \text{O}_3] \\
& + n_5 y_1 H[(\text{Mg}_{1-x_4} \text{Fe}_{x_4}^{3+, \text{HS}}) (\text{Si}_{1-x_4} \text{Fe}_{x_4}^{3+, \text{HS}}) \text{O}_3] + n_5 (1-y_1) H[(\text{Mg}_{1-x_4} \text{Fe}_{x_4}^{3+, \text{HS}}) (\text{Si}_{1-x_4} \text{Fe}_{x_4}^{3+, \text{LS}}) \text{O}_3] \\
& + n_6 H[\text{Fe}^0] - n_1 x y T S_{\text{mag}}(\text{Fe}^{2+, \text{HS}}, \text{Fp}) - n_1 x (1-y) T S_{\text{mag}}(\text{Fe}^{2+, \text{LS}}, \text{Fp}) - \\
& n_2 x_1 T S_{\text{mag}}(\text{Fe}^{2+, \text{HS}}, \text{Pv, A-site}) - (n_4 x_3 + n_5 x_4) T S_{\text{mag}}(\text{Fe}^{2+, \text{HS}}, \text{Pv, A-site}) - \\
& n_5 x_4 y_1 T S_{\text{mag}}(\text{Fe}^{3+, \text{HS}}, \text{Pv, B-site}) - n_5 x_4 (1-y_1) T S_{\text{mag}}(\text{Fe}^{3+, \text{LS}}, \text{Pv, B-site}) - n_6 T S(\text{Fe}^0) \\
& - (n_2 + n_3 + n_4 + n_5) T S_{\text{config}}(\text{Pv, A-site}) - (n_2 + n_3 + n_4 + n_5) T S_{\text{config}}(\text{Pv, B-site}) \\
& - n_1 T S_{\text{config}}(\text{Fp, A-site})
\end{aligned} \tag{6}$$

$$S_{\text{config}}(\text{Pv, B-site}) = -k_B (X_{\text{Si}} \ln X_{\text{Si}} + X_{\text{Fe}, 3+, \text{HS}} \ln X_{\text{Fe}, 3+, \text{HS}} + X_{\text{Fe}, 3+, \text{LS}} \ln X_{\text{Fe}, 3+, \text{LS}} + X_{\text{Al}, 3+} \ln X_{\text{Al}, 3+}) \tag{7}$$

The mechanism for creating oxygen vacancies is not specifically considered in our modeling here as the oxygen vacancies have been predicted to be a very high energy defect (see our previous work [Xu *et al.*, 2015] for details).

4.3. Parameters for the DFT Calculations

Our ab initio calculations are performed using the Vienna ab initio simulation package (VASP) based on DFT. The projector-augmented wave (PAW) method [Blochl, 1994] is used for the effective potentials of all the atoms in the system. The PAW potentials we used included valence electrons $2p^6 3s^2$ for Mg, $3s^2 3p^2$ for Si, $2s^2 2p^4$ for O, $3p^6 3d^7 4s^1$ for Fe, and $3s^2 3p^1$ for Al. A cutoff energy of 600 eV is used to ensure that the plane wave basis is large enough for the calculations to converge.

It is well known that the normal Local Density Approximation (LDA) and Generalized Gradient Approximation (GGA) functionals often provide inaccurate energetics for transition metal oxides, including oxides containing Fe [Wang *et al.*, 2006]. All the calculations in this work are therefore performed with HSE06 hybrid functional [Heyd *et al.*, 2003; Paier *et al.*, 2006] as implemented in the VASP code. The fraction of the exact Hartree-Fock exchange functional is set to be 0.25 (i.e., we set AEXX = 0.25 in the INCAR file). The HSE06 functional has been shown to yield significantly more accurate energetics for transition metal redox reactions than standard LDA or GGA techniques [Chevrier *et al.*, 2010]. All details concerning the k points and supercell setup information are shown in SI Table S3 [Dubrovinsky *et al.*, 2000]. The choices of the k point mesh yield a convergence of the total energy of a supercell within 1 meV/atom, while the structural relaxation is converged to less than 10^{-3} eV in the total energy, yielding the average forces between atoms to be about 0.01 eV/Å. The validation of our ab initio calculations for these high-pressure phases in comparison with experimental equation of states (EOS) is shown in SI section 3.1 [Birch, 1986; Catalli *et al.*, 2011b; Catalli *et al.*, 2010; Dubrovinsky *et al.*, 2000; Fiquet *et al.*, 2000; Jacobsen *et al.*, 2002; Lin *et al.*, 2013, 2005; Lundin *et al.*, 2008; Mao *et al.*, 2011; Mathon *et al.*, 2004; Speziale *et al.*, 2001]. It should be noted here that among all the DFT calculated energies of the end-members in our thermodynamic model, two of them are obtained based on semiempirical approaches. The first one is the enthalpy of metallic Fe as a function of pressures, where the experimental EOS parameters are used. The other one is the enthalpy of LS Fp ($\text{Mg, Fe}^{\text{LS}}\text{O}$) as a function of pressures, where a constant energy shift is applied to match with previous experimental and theoretical results of the spin transition region (please refer to SI section 3.1 for details [Lin *et al.*, 2013; Tsuchiya *et al.*, 2006]).

4.4. Density and Bulk Modulus of the Lower Mantle Phases

To calculate the density and bulk modulus of the lower mantle phases along an expected geotherm [Brown and Shankland, 1981], we have considered high-temperature effects on the volume and bulk modulus of the solid end-members in the system at high pressures. It should be noted here that the thermal expansion influence is not included in our Gibbs energy minimization calculation to find the equilibrium state of the system. After we get the different end-members contents in equilibrium, we consider the high-temperature effects on volume and bulk modulus to correct our corresponding DFT values $V(P)^{\text{DFT}}$, isothermal $K_T(P)^{\text{DFT}}$. Then we calculate the adiabatic bulk modulus K_S for the bulk sound velocity calculation. After we obtain the density and the adiabatic bulk modulus of each lower mantle phase, the Voigt-Reuss-Hill average is used to calculate the bulk modulus of the lower mantle [Lu *et al.*, 2013; Murakami *et al.*, 2012]. Please refer to

the SI section 4.2 for the calculation details of the lower mantle density, bulk modulus, and bulk sound velocity.

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