

# Thermal equation of state of natural tourmaline at high pressure and temperature

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**Abstract** Synchrotron-based in situ angle-dispersive X-ray diffraction experiments were conducted on a natural uvite-dominated tourmaline sample by using an external-heating diamond anvil cell at simultaneously high pressures and temperatures up to 18 GPa and 723 K, respectively. The angle-dispersive X-ray diffraction data reveal no indication of a structural phase transition over the P–T range of the current experiment in this study. The pressure–volume–temperature data were fitted by the high-temperature Birch–Murnaghan equation of state. Isothermal bulk modulus of  $K_0 = 96.6$  (9) GPa, pressure derivative of the bulk modulus of  $K'_0 = 12.5$  (4), thermal expansion coefficient of  $\alpha_0 = 4.39$  (27)  $\times 10^{-5}$  K<sup>-1</sup> and temperature derivative of the bulk modulus  $(\partial K/\partial T)_P = -0.009$  (6) GPa K<sup>-1</sup> were obtained. The axial thermoelastic properties were also obtained with  $K_{a0} = 139$  (2) GPa,  $K'_{a0} = 11.5$  (7) and  $\alpha_{a0} = 1.00$  (11)  $\times 10^{-5}$  K<sup>-1</sup> for the *a*-axis, and  $K_{c0} = 59$  (1) GPa,  $K'_{c0} = 11.4$  (5) and  $\alpha_{c0} = 2.41$  (24)  $\times 10^{-5}$  K<sup>-1</sup> for the *c*-axis. Both of axial compression and thermal expansion exhibit large anisotropic behavior. Thermoelastic parameters of tourmaline in this study were also

compared with that of the other two ring silicates of beryl and cordierite.

**Keywords** Equation of state · Tourmaline · Diamond anvil cell · High-temperature and high-pressure · X-ray diffraction

## Introduction

Tourmaline is the term of a supergroup which covering several closely related minerals rather than a single mineral (Henry et al. 2011). This group of minerals has a complex general chemical formula with  $XY_3Z_6[T_6O_{18}][BO_3]_3V_3W$ , where  $X = K^+$ ,  $Na^+$ ,  $Ca^{2+}$ ,  $Pb^{2+}$ , vacancy,  $Y = Li^+$ ,  $Mg^{2+}$ ,  $Ti^{4+}$ ,  $Al^{3+}$ ,  $Mn^{3+}$ ,  $Cr^{3+}$ ,  $V^{3+}$ ,  $Fe^{3+}$ ,  $Fe^{2+}$ ,  $Mn^{2+}$ ,  $Cu^{2+}$ ,  $Z = Mg^{2+}$ ,  $Fe^{2+}$ ,  $Fe^{3+}$ ,  $V^{3+}$ ,  $Cr^{3+}$ ,  $Al^{3+}$ ,  $T = Si^{4+}$ ,  $B^{3+}$ ,  $Al^{3+}$ ,  $B = B^{3+}$ ,  $V = OH^-$ ,  $O^{2-}$  and  $W = O^{2-}$ ,  $F^-$ ,  $OH^-$  (Hawthorne and Dirlam 2011). Recently, Wunder et al. (2015) found that the *X* site can also be occupied by  $[NH_4]^+$  in their synthetic ammonium-bearing tourmaline. Tourmaline has a trigonal crystal system with space group of  $R3m$  (Fig. 1), the cyclosilicate structure is formed by six corner-shared  $TO_4$  tetrahedra, and the *T* site is mainly occupied by Si, although the substitutions of B (e.g., Hughes et al. 2000; Schreyer et al. 2000) and Al (Rosenberg and Foit 1979) for Si exist. In addition, boron occupies the triangularly coordinated *B* site. Meanwhile, the *Y* and *Z* sites are both octahedrally coordinated and the *X* site is nine-coordinated. Tourmaline has been widely used in many areas. For instance, fantastic colors and hardness make it a spectacular gemstone. Its other physical properties such as pyroelectricity and piezoelectricity can be used in the manufacture of pressure gauges and other electronic components (Nesse 2000).

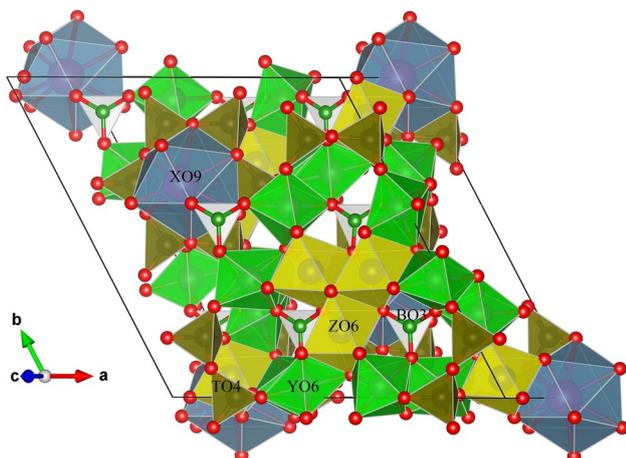
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**Fig. 1** Crystal structure of tourmaline. (*Color online*)

Tourmaline also plays an important role in geosciences. It can exist in igneous rocks (usually in highly chemical fractionated rocks such as granitic pegmatites, granite and granodiorite), sedimentary rocks (its high resistance during weathering makes it a clastic component in sediment) and metamorphic rocks (commonly formed from preexisting tourmaline detrital grains and diagenetic cores) as a minor or accessory mineral (van Hinsberg et al. 2011a). It also is known as a major mineral in tourmalinites (Slack 1996). Its complexity in composition gives the geological history information of incomparably large range of different elements (Marschall and Jiang 2011), since element diffusion in its structure is negligible (van Hinsberg et al. 2011b), and it is stable over a wide pressure and temperature range from near surface (Henry et al. 1999) to mantle conditions (Krosse 1995; Ota et al. 2008a; Marschall et al. 2009). Since tourmaline is extensively existed in many hydrothermal ore deposits such as mesothermal gold, sulfide and uranium deposits (Slack and Trumbull 2011), the isotope systematic of tourmaline is widely used to identify likely fluid sources for ore genesis (e.g., Palmer and Slack 1989; Taylor et al. 1992, 1999; Jiang et al. 2002). In addition, due to its slow volume diffusion (Henry and Dutrow 1996; Desbois and Ingrin 2007), large grain size and recognizable growth zones (Marschall and Jiang 2011), tourmaline is also a utility isotopic clock in geochronology.

It is generally believed that the components from the slab are probably brought by fluids to the mantle wedge in deep subduction zones, which induce partial melting and the forming of island arc magmas (e.g., Perfit et al. 1980; Saunders et al. 1980; Nakamura et al. 1985). Therefore, to investigate the nature of the subducting slabs is significant for understanding the crust–mantle recycling in subduction zones (Moriguti et al. 2004). The light elements

lithium and boron are widely used as the important geochemical tracers for crust–mantle recycling at subduction zones (e.g., Chan et al. 1999; Nakano and Nakamura 2001; Chan et al. 2002; Bebout and Nakamura 2003; Zack et al. 2003), mainly due to their incompatibilities during melting (Ryan and Langmuir 1987; Brenan et al. 1998a), high fluid-mobility (e.g., Seyfried et al. 1984; Bebout et al. 1993; Ryan and Langmuir 1993; Brenan et al. 1998b) and easy-fractionating stable isotopes at low temperature (Moriguti et al. 2004). Tourmaline, as a dominant carrier of boron and lithium, and found in many rock types (e.g., Henry and Dutrow 1996; Nakano and Nakamura 2001; Busigny and Bebout 2013), is an important mineral which gives particular information about the chemical evolution of materials in subduction zones (Nakano and Nakamura 2001; Bebout and Nakamura 2003; Moriguti et al. 2004; Ota et al. 2008a, b). Consequently, studying the stability of tourmaline is important to build a basis for assessing the depth in which boron is still incorporated in tourmaline at subduction zones and explaining the anomaly of boron isotopes in basaltic volcanic rocks (Moriguti et al. 2004). For a single synthetic tourmaline end-member, dravite decomposes at temperature 900 °C, 6–8 GPa, and at 3–5 GPa, >1000 °C (Krosse 1995; Werding and Schreyer 1996). In the presence of SiO<sub>2</sub>, however, tourmaline decomposes between 4 and 4.5 GPa at 800 °C and between 4.5 and 5 GPa at 700 °C (Ota et al. 2008a).

In this paper, we have investigated the stability of a natural tourmaline sample at high pressures (up to ~18 GPa) and relatively low temperatures (up to 723 K) using an external-heating diamond anvil cell combined with in situ synchrotron radiation angle-dispersive X-ray diffraction. The purpose is to identify the stability of tourmaline at high pressure and relatively low temperature. Although tourmaline has been proved to be stable at pressures lower than 8 GPa at high temperatures (>700 °C) by previous studies (Krosse 1995; Werding and Schreyer 1996; Ota et al. 2008a), there has been no detailed study on its stabilities at high pressures and relatively low temperatures. Investigation of tourmaline at these *P–T* conditions is significant for its application in geosciences, since cold conditions within slabs still exist to preserve colder slab temperatures to greater depths, for instance, at the coldest part of an old and fast subducting slab which can retain a relatively low temperature (~700 K) to a depth of ~540 km according to Bina and Navrotsky (2000), because the thermal evolution of the slab is strongly affected by the rate and the age of the subducting slab (Kincaid and Sacks 1997). In addition, despite the geothermobarometric potential of tourmaline (van Hinsberg and Schumacher 2009), its thermodynamic data are still limited. Consequently, the thermoelastic property of tourmaline was obtained by fitting the experimental *P–V–T* data and compared with previous studies and then

discussed the possibility of tourmaline along with subducting slab into deeper Earth.

## Sample and experimental methods

A natural tourmaline sample was collected from Pakistan. The pure tourmaline grains were grounded in an agate mortar for 4–6 h to obtain a fine powder (a few microns). We used conventional powder X-ray diffraction method to examine the ground powder, after being heated at 50 °C in a constant temperature furnace for 2 h to eliminate the absorbed water. The ambient X-ray diffraction data were collected using a D/Max-2200 diffractometer with a graphite crystal monochromator and CuK $\alpha$  radiation. The spectrum was indexed using the standard spectrum (JCPDS 71-0716), confirming the structure is trigonal and belong to the space group of  $R3m$ . The data of conventional diffraction collected at ambient condition give the parameters  $a = 15.823$  (6) Å,  $c = 7.089$  (4) Å and  $V = 1537.1$  (11) Å<sup>3</sup>. Chemical analysis based on electron microprobe technique showed that this tourmaline sample is uvite-dominated with a chemical formula of  $[(Ca_{0.86}Na_{0.11}\square_{0.03})Mg_3(Al_{0.86}Mg_{0.09}V_{0.02})_6(Si_6O_{18})(BO_3)_3(OH)_3F]$ , and the water content is constrained to be 2.43 wt%, assuming the molar ratio of H:O to be 1:10 (e.g., Ye et al. 2015).

Pressures up to 18.4 GPa were generated by a modified Merrill–Bassett-type diamond anvil cell (DAC) equipped with two 500- $\mu$ m culet-size diamond anvil. A rhenium gasket was pre-indented to a  $\sim 70$   $\mu$ m thickness before laser drilling of a 200- $\mu$ m-diameter hole. The tourmaline sample powder was mixed with 1.0 wt% gold powder which was used as the pressure calibrant. The mixture of these two powders was slightly pressed to form a disk of  $\sim 25$   $\mu$ m thickness, and then, a piece of this disk about 100  $\mu$ m in diameter was loaded into the sample chamber. The pressure-transmitting medium was a mixture of ethanol–methanol–water (16:3:1), and the equation of state of gold (pressure marker) served as the pressure calibration (Fei et al. 2007). Temperatures up to 723 K were generated by a resistance-heating system and measured by a NiCr–NiSi thermocouple which was attached to the diamond. The experimental setup and cell assembly were described in detail by Fan et al. (2010).

High-pressure and high-temperature angle-dispersive X-ray diffraction was performed in situ at the 4W2 beamline of the Beijing Synchrotron Radiation Facility (BSRF), and diffraction images were acquired on a MAR-345 detector. The incident X-ray beam was monochromatic with a wavelength of 0.6199 Å which was calibrated by scanning through the Mo metal K-absorption edge. The X-ray beam was focused to a beam size of  $35 \times 14$   $\mu$ m<sup>2</sup> FWHM by two mirrors in the Kirkpatrick–Baez configuration. The tilting and rotation of

the detector relative to the X-ray beam were calibrated using cerium dioxide (CeO<sub>2</sub>) powder as the diffraction standard, so did the distance between sample and detector. Diffraction patterns were integrated and treated using the Fit2D (Hammersley 1996) and EXPGUI/GSAS (Toby 2001; Larson and Von Dreele 2004). The unit cell parameters of the sample and the pressure calibrant (gold) were both achieved by reducing full diffraction patterns following the LeBail method (Le Bail et al. 1988), and a typical fitting of the full diffraction pattern at 14.8 GPa and 573 K was shown in Fig. 2.

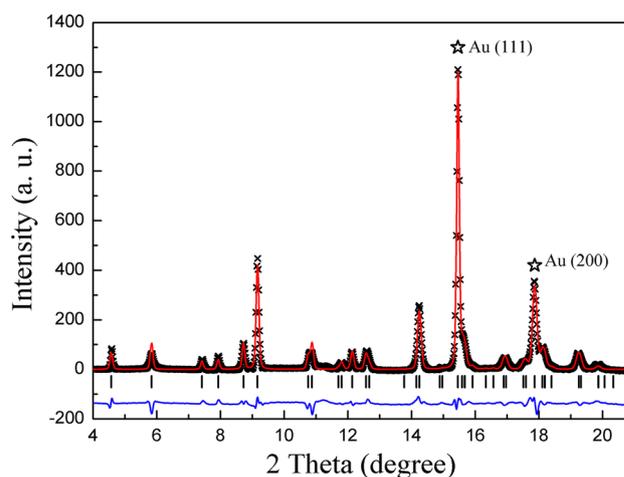
## Results and discussion

### Equation of State at 300 K

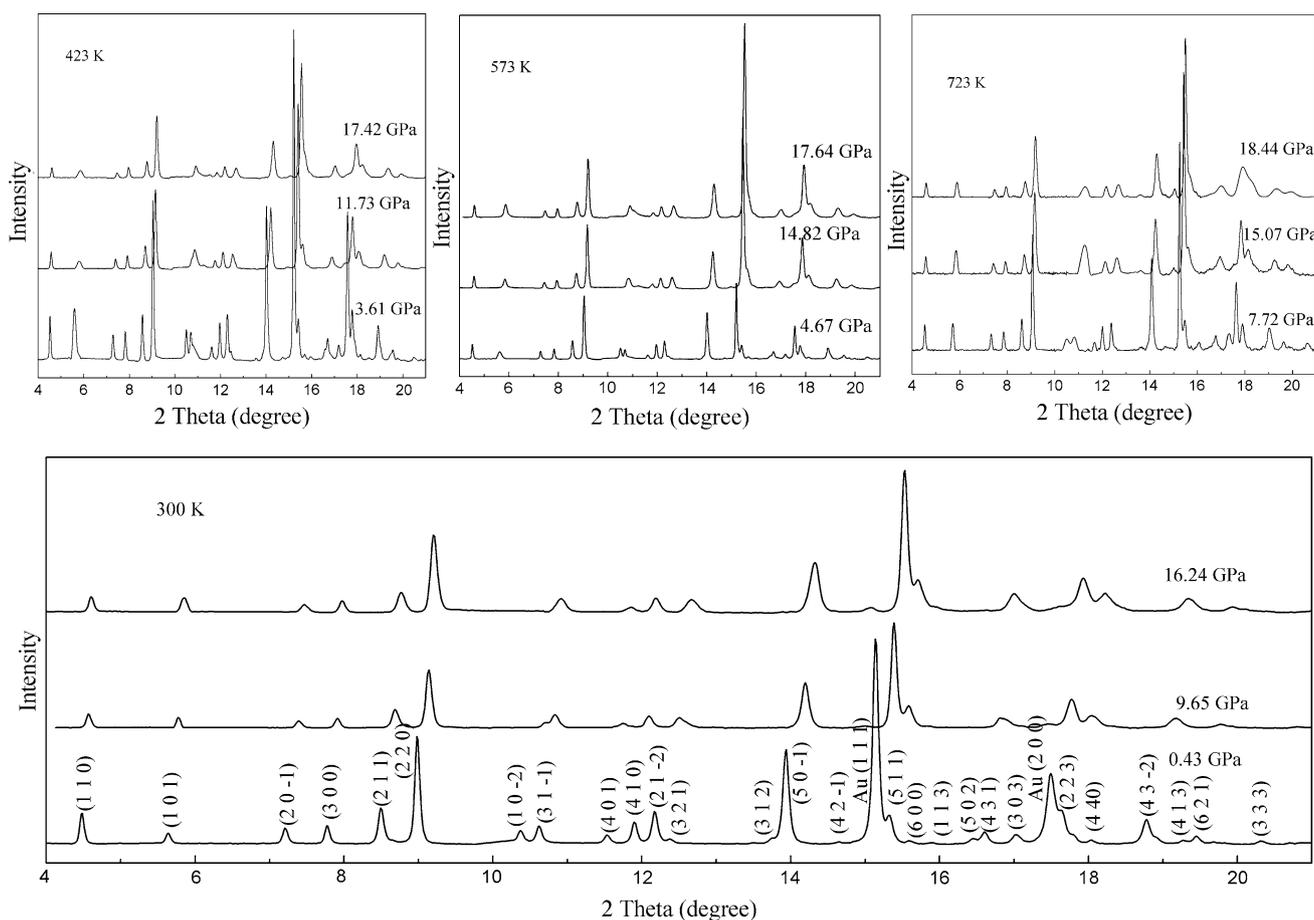
No phase transition was observed throughout the whole range of pressure and temperature performed in this study based on the X-ray diffraction patterns (Fig. 3). The variations of the d-spacings with pressures are continuous, which can also prove that tourmaline is stable within this pressure and temperature range in this study (Fig. 4). Table 1 shows the unit cell parameters and volumes of tourmaline at various pressures and temperatures. We first fitted the pressure–volume data at 300 K with the third-order Birch–Murnaghan (III-BM) EoS (Birch 1947) to obtain the isothermal bulk modulus and its pressure derivative:

$$P = (3/2)K_0 \left[ (V_0/V)^{7/3} (V_0/V)^{5/3} \right] \times \left\{ 1 + (3/4)(K'_0/4) \left[ (V_0/V)^{2/3} - 1 \right] \right\} \quad (1)$$

where  $V_0$ ,  $V$ ,  $K_0$  and  $K'_0$  are the zero-pressure volume, high-pressure volume, isothermal bulk modulus and its



**Fig. 2** Le Bail profile fitting of the diffraction profiles at 14.82 GPa and 573 K. Observed spectra (black line), fitted spectra (red solid line), difference plot (blue solid line) and Bragg peak positions (tick marks) are shown. (Color online)



**Fig. 3** Representative X-ray diffraction patterns of tourmaline obtained in this study at different pressures and temperatures of 300, 423, 573 and 723 K

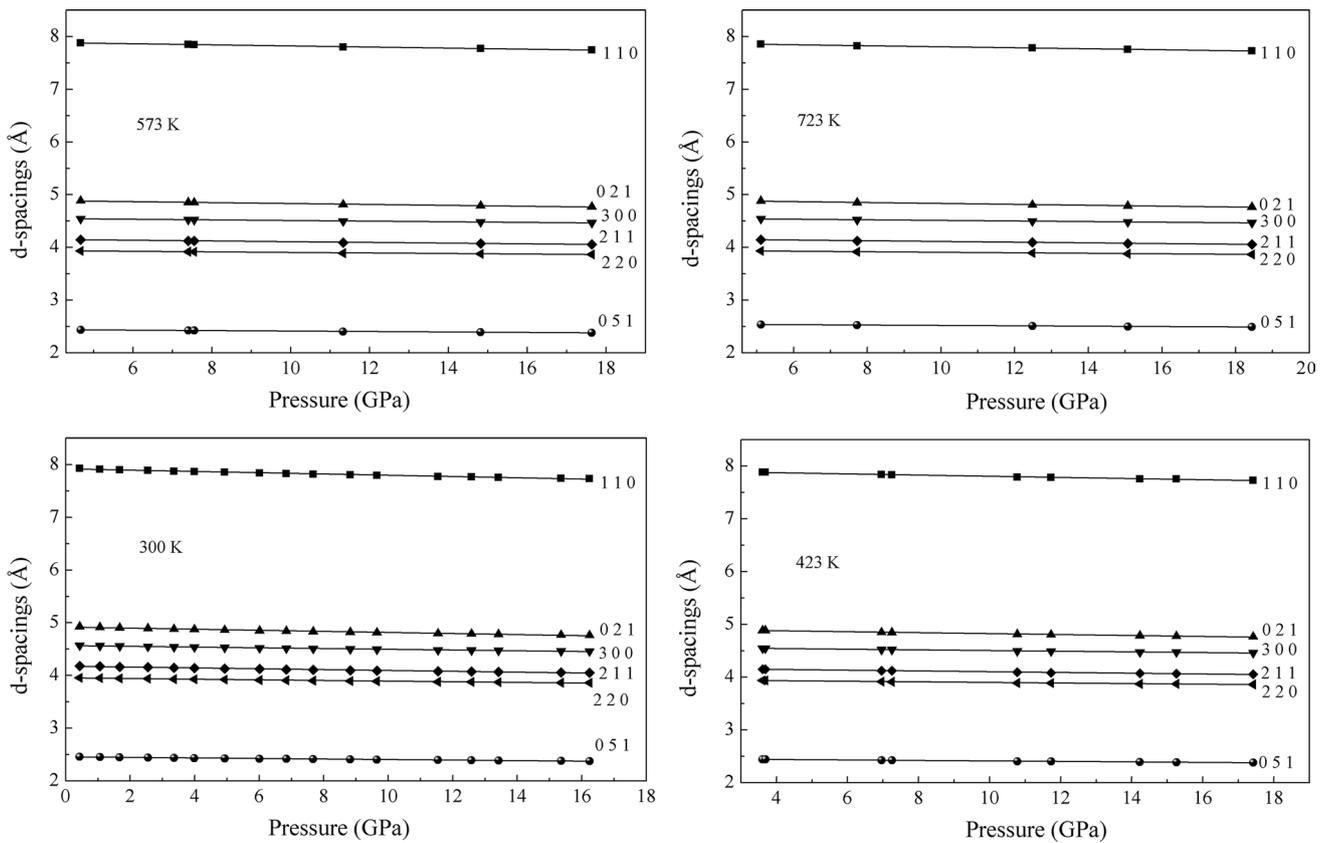
pressure derivative, respectively. The least square fitting yielded  $K_0 = 97$  (1) GPa, and  $K'_0 = 12.4$  (4). When fixing  $K'_0 = 4$ , the isothermal bulk modulus was determined as 120 (2) GPa, respectively. The unit cell volume data at 300 K as a function of pressure and the compression curve calculated from these fitted parameters are shown in Fig. 5.

The evolution of the lattice parameters as a function of pressure exhibits a large anisotropy (Fig. 6). The lattice parameters were fitted to a linearized III-BM EoS (Angel 2000) to obtain the linear EoS parameters, yielding:  $K_{a0} = 138$  (2) GPa and  $K'_{a0} = 11.8$  (6) for the  $a$ -axis and  $K_{c0} = 60$  (1) GPa and  $K'_{c0} = 10.9$  (5) for the  $c$ -axis. We also calculated the axial compressibilities (with  $\beta_d = 1/3K_0$ , where  $K_0$  is the isothermal bulk modulus at ambient conditions,  $\beta$  is the compressibility and  $d$  is the unit cell parameter) and obtained  $\beta_a = 2.4 \times 10^{-3}$  GPa $^{-1}$  and  $\beta_c = 5.6 \times 10^{-3}$  GPa $^{-1}$  for  $a$ - and  $c$ -axis, respectively. The elastic anisotropy can be expressed as:  $\beta_a : \beta_c = 1.00 : 2.30$ .

Figure 7 shows the axial and volume Eulerian finite strain (for unit cell volume,  $f_{EV} = [(V_0/V)^{2/3} - 1]/2$ , and for lattice parameters) versus

“normalized pressure” ( $F_{EV} = P/[3f_{EV}(2f_{EV} + 1)^{5/2}]$ , and  $F_{Ea} = P/[3f_{Ea}(2f_{Ea} + 1)^{5/2}]$  plots [ $f_E - F_E$  plot; (Angel 2000)]. The weighted linear fit of the data points yields the intercept values of  $F_{Ea}(0) = 135$  (2) GPa for the  $a$ -axis,  $F_{Ec}(0) = 61$  (1) GPa for the  $c$ -axis and  $F_{EV}(0) = 96.3$  (8) GPa for the unit cell volume. It is clear from Fig. 7 that the data points lie on an inclined straight line with a relatively large positive slope, showing that the III-BM EoS is a reasonable description of the  $P$ - $V$  data (e.g., Angel 2000; Burt et al. 2006; Nestola et al. 2010). Furthermore, the normalized stress values obtained at  $f_E = 0$  are consistent with the axial and volume bulk moduli determined by the III-BM EoS.

The Vinet EoS (Vinet et al. 1986, 1987) was also used to analyze the  $P$ - $V$  data at 300 K. The expression for the Vinet EoS is:  $P(V) = 3K_0y^{-2}(1-y)\exp[\eta_0(1-y)]$ , where  $y = x^{1/3}$ ,  $x = V/V_0$  and  $\eta_0 = (3/2)(K'_0 - 1)$ . Analyses with all parameters free yield the values of  $K_0 = 98$  (1) GPa and  $K'_0 = 11.3$  (3), which are close to that of  $K_0 = 97$  (1) GPa, and  $K'_0 = 12.4$  (4) derived by the fitting to BM EoS within their uncertainties.



**Fig. 4** Pressure dependence of the d-spacings of several crystallographic planes in tourmaline at temperatures of 300, 423, 573 and 723 K

### High-temperature EoS

The high-temperature III-BM EoS:

$$P = (3/2)K_{T0} \left[ (V_{T0}/V)^{7/3} (V_{T0}/V)^{5/3} \right] \times \left\{ 1 + (3/4)(K'_{T0}/4) \left[ (V_{T0}/V)^{2/3} - 1 \right] \right\} \quad (2)$$

where  $K_{T0}$ ,  $K'_{T0}$  and  $V_{T0}$  are bulk modulus, its pressure derivative and the unit cell volume at ambient pressure and temperature (in Kelvin), which was used to fit the  $P$ – $V$ – $T$  data in Table 1.  $V_{T0}$  (thermal dependences of the zero-pressure volume) and bulk modulus  $K_{T0}$  at different isotherms given by the following expressions:

$$V_{T0} = V_0 \exp \int_{300}^T \alpha_T dT \quad (3)$$

$$K_{T0} = K_0 + (\partial K_{T0} / \partial T)_P \times (T - 300) \quad (4)$$

where  $V_0$ ,  $\alpha_T$  and  $K_0$  are the unit cell volume at ambient conditions, thermal expansion at temperature and ambient pressure and values of bulk modulus at ambient conditions. Generally, thermal expansion shall be assumed to be a linear function of temperature ( $\alpha_T = \alpha_0 + \alpha_1 T$ ) (e.g.,

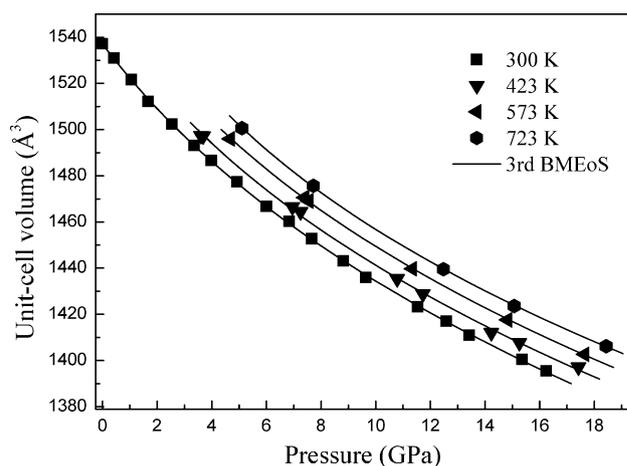
Liu et al. 2014). However, in view of the relatively low-temperature range (~723 K) and the limited high-pressure and temperature data points in this study, it is difficult to obtain reasonable result of  $\alpha_1$  (Nishihara et al. 2003). Therefore,  $(\partial K_{T0} / \partial T)_P$  and  $\alpha_T$  were assumed to be constant over the temperature range in this study (Nishihara et al. 2003). By doing so, using the console program, EosFit7c (Angel et al. 2014), we obtained:  $K_0 = 96.6$  (9) GPa,  $K'_0 = 12.5$  (4),  $(\partial K / \partial T)_P = -0.009$  (6) GPa K<sup>-1</sup> and  $\alpha_0 = 4.39$  (27)  $\times 10^{-5}$  K<sup>-1</sup>. The values of bulk modulus  $K_0$  and its derivative  $K'_0$  determined here are in good agreement with that derived from fitting of  $P$ – $V$  data at 300 K. Figure 5 shows the evolution of cell volume with pressure and temperature as well as the isotherms calculated using the thermoelastic parameters. In addition, we also applied a “linearized” III-BM EoS with the EosFit7c program to calculate the linear thermoelastic parameters of this tourmaline sample, and we obtained:  $K_{a0} = 139$  (2) GPa,  $K'_{a0} = 11.5$  (7) and  $\alpha_{a0} = 1.00$  (11)  $\times 10^{-5}$  K<sup>-1</sup> for the  $a$ -axis and  $K_{c0} = 59$  (1) GPa,  $K'_{c0} = 11.4$  (5) and  $\alpha_{c0} = 2.41$  (24)  $\times 10^{-5}$  K<sup>-1</sup> for the  $c$ -axis.

To estimate the impact of non-hydrostatic compression to the results of elastic parameters derived from EoS fit, we calculated the bulk modulus ( $K_0$ ) and its pressure derivative

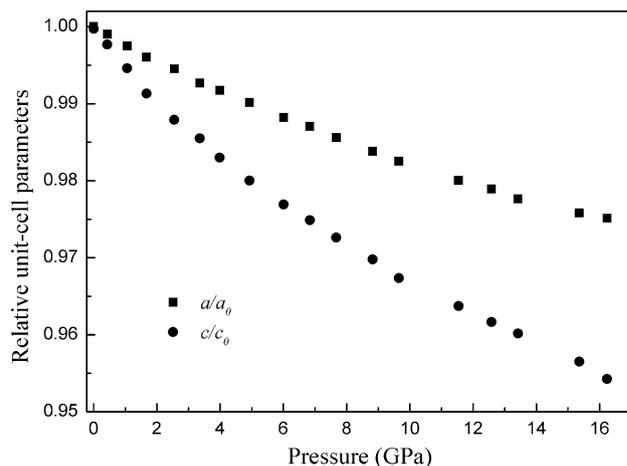
**Table 1** Unit cell parameters of tourmaline at various  $P$ – $T$  conditions

$P$ (GPa)	$T$ (K)	$a$ (Å)	$c$ (Å)	$V$ (Å <sup>3</sup> )
0.0001	300	15.823 (6)	7.089 (4)	1537.1 (11)
0.4 (0)	300	15.8073 (2)	7.0746 (3)	1530.89 (7)
1.1(1)	300	15.7834 (3)	7.0529 (4)	1521.61(9)
1.7 (1)	300	15.7606 (3)	7.0295 (4)	1512.17 (10)
2.6 (1)	300	15.7365 (3)	7.0054 (5)	1502.37 (11)
3.4 (2)	300	15.7070 (5)	6.9883 (7)	1493.11 (15)
4.0 (2)	300	15.6923 (5)	6.9706 (8)	1486.53 (19)
4.9 (3)	300	15.6677 (4)	6.9495 (9)	1477.39 (20)
6.0 (3)	300	15.6361 (5)	6.9273 (11)	1466.73 (24)
6.8 (3)	300	15.6178 (4)	6.9129 (8)	1460.24 (19)
7.7 (4)	300	15.5953 (4)	6.8970 (9)	1452.70 (20)
8.8 (4)	300	15.5668 (6)	6.8767 (11)	1443.13 (25)
9.7 (5)	300	15.5468 (8)	6.8596 (11)	1435.86 (25)
11.5 (6)	300	15.5072 (6)	6.8339 (12)	1423.19 (26)
12.6 (6)	300	15.4899 (7)	6.8191 (15)	1416.96 (33)
13.4 (7)	300	15.4692 (7)	6.8085 (14)	1410.97 (32)
15.4 (8)	300	15.4403 (7)	6.7826 (18)	1400.40 (40)
16.2 (8)	300	15.4296 (12)	6.7666 (27)	1395.10 (60)
3.6 (2)	423	15.7250 (4)	6.9924 (5)	1497.40 (12)
3.7 (2)	423	15.7242 (4)	6.9921 (5)	1497.20 (12)
7.0 (4)	423	15.6371 (4)	6.9253 (7)	1466.51 (15)
7.3 (4)	423	15.6330 (5)	6.9190 (8)	1464.40 (18)
10.8 (5)	423	15.5415 (4)	6.8618 (8)	1435.33 (18)
11.7 (6)	423	15.5313 (7)	6.8394 (19)	1428.80 (40)
14.2 (7)	423	15.4724 (6)	6.8109 (11)	1412.04 (25)
15.3 (8)	423	15.4711 (6)	6.7911 (15)	1407.70 (32)
17.4 (9)	423	15.4245 (8)	6.7805 (19)	1397.10 (40)
4.7 (2)	573	15.7183 (3)	6.9918 (5)	1496.00 (11)
7.4 (4)	573	15.6564 (5)	6.9278 (9)	1470.64 (19)
7.6 (4)	573	15.6468 (4)	6.9293 (7)	1469.15 (17)
11.3 (6)	573	15.5642 (7)	6.8625 (14)	1439.68 (30)
14.8 (7)	573	15.4986 (5)	6.8145 (12)	1417.59 (26)
17.6 (9)	573	15.4513 (6)	6.7842 (13)	1402.67 (29)
5.1 (3)	723	15.730 (3)	7.003 (6)	1500.7 (10)
7.7 (4)	723	15.676 (6)	6.934 (7)	1475.7 (14)
12.5 (6)	723	15.590 (6)	6.839 (7)	1439.5 (14)
15.1 (8)	723	15.522 (3)	6.823 (5)	1423.6 (8)
18.4 (9)	723	15.471 (3)	6.784 (5)	1406.2 (8)

( $K'_0$ ) from fitting the  $P$ – $V$  data within 10 GPa at room temperature and obtained:  $K_0 = 97$  (1) GPa and  $K'_0 = 12.6$  (7), which is consistent with the results of fitting all room temperature data that lead to  $K_0 = 97$  (1) GPa, and  $K'_0 = 12.4$  (4). Likewise, the thermoelastic parameters calculated from the  $P$ – $V$ – $T$  data within 10 GPa were also determined as:  $K_0 = 96$  (1) GPa,  $K'_0 = 12.8$  (7),  $(\partial K/\partial T)_P = -0.008$  (13) and  $\alpha_0 = 4.35$  (49)  $\times 10^{-5}$  K<sup>-1</sup>, similarly, coincide with results from all  $P$ – $V$ – $T$  data [ $K_0 = 96.6$  (9) GPa,



**Fig. 5** Unit cell volume of tourmaline as a function of pressure and temperature. The *solid lines* represent isothermal compression curve calculated from thermoelastic parameters. The *error bars* of the data points are smaller than the *symbols*

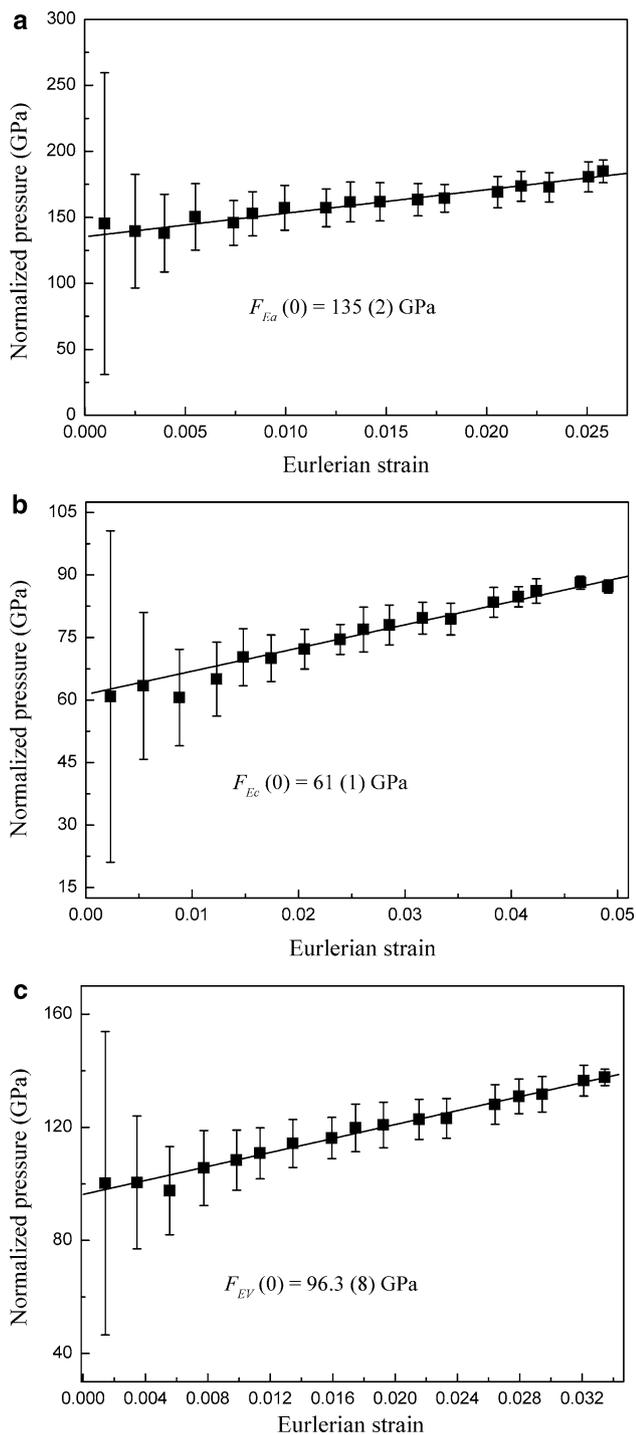


**Fig. 6** Pressure dependence of the unit cell parameters  $a$  and  $c$  of tourmaline in this study. Note that the *symbols* are larger than the *uncertainties*

$K'_0 = 12.5$  (4),  $(\partial K/\partial T)_P = -0.009$  (6) and  $\alpha_0 = 4.39$  (27)  $\times 10^{-5}$  K<sup>-1</sup>]. Therefore, the influence of non-hydrostatic stress on the thermoelastic parameters is limited in this study.

### Cation effects on the compressibility

Schorl is another tourmaline species with Na<sup>+</sup>, Fe<sup>2+</sup> and Al<sup>3+</sup> occupying X, Y and Z site, respectively, and its compressional property was examined by Li et al. (2004) using powder X-ray diffraction method in a DAC at high pressure (up to 27.8 GPa) and room temperature; they obtained the isothermal bulk modulus [ $K_0 = 183.5$  (4.2) GPa] with  $K'_0$  constrained to be 4 (Table 2). In this study, the isothermal



**Fig. 7** Volume Eulerian strain-normalized pressure ( $F_E - f_E$ ) plot of **a** lattice parameter, **b** *c* lattice parameter and **c** unit cell volume. The solid line represents the linear fit through the data

bulk modulus of uvite [ $K_0 = 97 (1) \text{ GPa}$ ,  $K'_0 = 12.4 (4)$ , when fixing  $K'_0 = 4$ ,  $K_0 = 120 (2) \text{ GPa}$ ] is smaller than that of schorl. This difference could be explained by the compositional difference between them. The chemical analysis of this tourmaline sample showed that it is uvite-dominated

$[(\text{Ca}_{0.86}\text{Na}_{0.11}\square_{0.03})\text{Mg}_3(\text{Al}_{0.86}\text{Mg}_{0.09}\text{V}_{0.02})_6(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{F}]$  with *X*, *Y* and *Z* site mainly occupied by  $\text{Ca}^{2+}$ ,  $\text{Mg}^{2+}$  and  $\text{Al}^{3+}$ . And that about 11 % of  $\text{Na}^+$  and 3 % of vacancies exist in *X* site and *Z* site is also contains 9 % of  $\text{Mg}^{2+}$  and 2 % of  $\text{V}^{3+}$ . The effective ionic radius (IR) of  $\text{Mg}^{2+}$  (VI) ( $\text{IR}_{\text{Mg(VI)}} = 0.72 \text{ \AA}$ ) at *Y* site in uvite is close to that of  $\text{Fe}^{2+}$  ( $\text{IR}_{\text{Fe(VI)}} = 0.78 \text{ \AA}$ ) in schorl (Shannon 1976) ( $\text{Fe}^{2+}$  is energetically favorable for the high spin state in silicates and oxides under ambient conditions (e.g., Lin and Tsuchiya 2008), so we selected the  $\text{IR}_{\text{Fe(VI)}}$  of high spin state); however, at the *Z* site 9 % of  $\text{Mg}^{2+}$  and 2 % of  $\text{V}^{3+}$  substitute part of  $\text{Al}^{3+}$ , both of  $\text{Mg}^{2+}$  and  $\text{V}^{3+}$  have much larger IRs ( $\text{IR}_{\text{Mg(VI)}} = 0.720 \text{ \AA}$  and  $\text{IR}_{\text{V(VI)}} = 0.640 \text{ \AA}$ ) than that of  $\text{Al}^{3+}$  ( $\text{IR}_{\text{Al(VI)}} = 0.535 \text{ \AA}$ ) (Shannon 1976), which likely results in a smaller isothermal bulk modulus of uvite than that of schorl. In addition, vacancies in *X* site would be also a possible attribution to the larger compressibility of uvite. A dravite-dominated sample [ $\text{NaMg}_3\text{Al}_6(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{OH}$ ], which is generally occurred in subduction zone settings, has  $\text{Al}^{3+}$  mainly on *Z* site, possibly has a larger isothermal bulk modulus than that of uvite since  $\text{IR}_{\text{Al(VI)}} (0.535 \text{ \AA})$  is smaller than  $\text{IR}_{\text{Mg(VI)}} (0.720 \text{ \AA})$  (Shannon 1976).

Additionally, Li et al. (2004) got the isothermal bulk modulus value of schorl with  $K'_0$  fixed at 4; however, in this study of uvite-dominated tourmaline, we obtained that  $K_0 = 97 (1) \text{ GPa}$  and  $K'_0 = 12.4 (4)$  with free  $K'_0$ , which indicates that fixing  $K'_0$  at 4 may be unreasonable to get a reliable value of  $K_0$  for tourmaline group minerals because of the large dependence between isothermal bulk modulus ( $K_0$ ) and its pressure derivative ( $K'_0$ ) (Bass et al. 1981). Consequently, this may be another reason for large difference (86.5 GPa) between  $K_0$  values of schorl and uvite. Last, the data used to calculate the EoS parameters covered from 0 to 27.8 GPa (Li et al. 2004); however, the pressure-transmitting medium mixed by methanol, ethanol and water is non-hydrostatic at pressures more than about 10 GPa without heating (Angel et al. 2007). Hence, the  $K_0$  value of schorl can be also influenced by the effect of non-hydrostatic stress. For this study of uvite, the impact of non-hydrostatic stress on the thermoelastic parameters was estimated to be limited which likely benefited from the heating during the experiment.

The  $K_0$  value of the tourmaline sample in this study is much smaller than that of beryl [ $[\text{Al}_2\text{Be}_3\text{Si}_6\text{O}_{18}]$ , hexagonal,  $K_0 = 180 (1) \text{ GPa}$ ] and cordierite [ $[\text{Mg}_2\text{Al}_3(\text{AlSi}_5\text{O}_{18})]$ , orthorhombic,  $K_0 = 131.0 (1.3) \text{ GPa}$ ] which belong to ring silicates group as well (Table 2). In the ring silicates group, the six corner-shared silicon tetrahedra ring is the basic structural building block. Beryl and cordierite have almost the same structure, but in cordierite structure one of the six tetrahedral site in the ring is occupied by  $\text{Al}^{3+}$  rather than  $\text{Si}^{4+}$ , and this reduces the symmetry (Nesse 2000). The smaller  $K_0$

**Table 2** Elastic parameters of tourmaline and other ring silicates (beryl and cordierite)

Sample	$V_0$ (Å <sup>3</sup> )	$K_0$ (GPa)	$K'_0$	Method	References
Schorl	1595.52 (1.98)	183.5 (4.2)	4 (fixed)	Powder XRD	Li et al. (2004)
Uvite	1537.1 (11)	96.6 (9)	12.5 (4)	Powder XRD	This study
		120 (2)	4 (fixed)		
Beryl	675.3 (2)	180 (1)	4.2 (fixed)	Powder XRD	Fan et al. (2015)
	675.63 (4)	179 (1)	3.7 (3)	Single XRD	Prencipe and Nestola (2005)
Cordierite	1551.97 (15)	131.0 (1.3)	−0.5 (0.4)	Single XRD	Miletich et al. (2014)

XRD X-ray diffraction

value of cordierite compared with that of beryl can be possibly explained by the larger metal cations ( $\text{Mg}^{2+}$  and  $\text{Al}^{3+}$ ) in its structure; the reason is that larger metal cations may cause large compressibilities for similar structural minerals (e.g., Zhang and Reeder 1999; Gao et al. 2014). For cordierite and beryl, the substitutions of  $\text{Mg}^{2+}$  for  $\text{Al}^{3+}$  in octahedral sites and  $\text{Al}^{3+}$  instead of  $\text{Be}^{2+}$  in tetrahedral site may cause a smaller  $K_0$  value of cordierite, because the IR of Mg ( $\text{VI}$ ) ( $\text{IR}_{\text{Mg(VI)}} = 0.720$  Å) is larger than that of Al ( $\text{VI}$ ) ( $\text{IR}_{\text{Al(VI)}} = 0.535$  Å) and the  $\text{IR}_{\text{Al(VI)}}$  (0.39 Å) is also larger than  $\text{IR}_{\text{Be(VI)}}$  (0.27 Å) (Shannon 1976). Compared with beryl and cordierite, the  $K_0$  value of the uvite sample in this study is much smaller (Table 2): one of the reasons may be the much larger cations ( $\text{IR}_{\text{Na(VI)}} = 1.24$  Å and  $\text{IR}_{\text{Ca(VI)}} = 1.18$  Å) in uvite, and the other reason is that the tourmaline structure contains  $[\text{OH}]^-$  group which can dramatically increase the compressibilities of minerals according to the previous studies (e.g., Lager et al. 2002; Smyth et al. 2005; Xu et al. 2014, 2015; Fan et al. 2013; Jacobsen 2006).

### Axial anisotropy of compressibility and thermal expansion in ring silicates minerals

The axial compressibility of the uvite sample shows the behavior of the  $c$ -axis direction being comparably softer than the  $a$ - and  $b$ -axis direction (Fig. 6) with a description of  $\beta_a = \beta_b = 2.4 \times 10^{-3}$  GPa<sup>−1</sup> and  $\beta_c = 5.6 \times 10^{-3}$  GPa<sup>−1</sup>. Similar anisotropic compression behaviors have been reported for experimental investigations on beryl [ $\beta_a = \beta_b = 1.59 \times 10^{-3}$  GPa<sup>−1</sup> and  $\beta_c = 2.36 \times 10^{-3}$  GPa<sup>−1</sup>; Fan et al. (2015)] as well as cordierite [ $\beta_a = \beta_b = 2.4 \times 10^{-3}$  GPa<sup>−1</sup> and  $\beta_c = 3.1 \times 10^{-3}$  GPa<sup>−1</sup>; Miletich et al. (2014)]. All of three common species of the ring silicates show the compression anisotropy with  $\beta_c > \beta_a = \beta_b$ , which can be explained by their characteristic sixfold rings which ranging along the directions parallel to  $c$ -axis. In the structures of beryl and cordierite, variable amounts of  $\text{H}_2\text{O}$  and other large alkali ions like  $\text{Na}^+$  can be contained in the center of the channels in the rings; likewise, for tourmaline, large ions (e.g.,  $\text{Na}^+$  and  $\text{Ca}^{2+}$ ) are also located along the axis of the column formed by tetrahedral rings. Therefore, the more

compressible  $c$ -axis may be caused by the water molecular and large ions along the  $c$ -axis. Comparing the  $\beta_a$ ,  $\beta_b$  and  $\beta_c$  of these three ring silicates, we find that the values of  $\beta_a$  and  $\beta_b$  ( $2.4 \times 10^{-3}$ ,  $1.59 \times 10^{-3}$  and  $2.4 \times 10^{-3}$  GPa<sup>−1</sup> for tourmaline in this study, beryl and cordierite, respectively) for three species are closer than that of  $\beta_c$  ( $5.7 \times 10^{-3}$ ,  $2.36 \times 10^{-3}$  and  $3.1 \times 10^{-3}$  GPa<sup>−1</sup> for tourmaline, beryl and cordierite); possibly, the smaller  $K_0$  value of tourmaline is mainly controlled by the compression of direction for the  $c$ -axis. The more compressible  $c$ -axis in tourmaline compared with beryl and cordierite may be caused by its larger amount of large ions.

Donnay (1977) measured the unit cell parameters of a elbaite sample by powder X-ray diffraction at room pressure and temperatures of 193 and 293 K, and the derived thermal expansion coefficient is  $4.56 \times 10^{-5}$  K<sup>−1</sup>. Thus, the thermal expansion coefficient of the tourmaline sample in this study [ $4.39 (27) \times 10^{-5}$  K<sup>−1</sup>] is in agreement with the result from Donnay (1977) (Table 3). The thermal coefficients of tourmaline with different compositions reported by Tatli and Pavlovic (1988) (method of dilatometry) and Pandey and Schreuer (2012) (method of strain gauge), however, are much too small for significant comparisons with that derived by X-ray diffraction method (Table 3). Compared with this tourmaline sample, the thermal expansion coefficient of another ring silicate beryl [ $\alpha_0 = 0.282 (74) \times 10^{-5}$  K<sup>−1</sup>; Fan et al. (2015)] is more than 10 times smaller, and the temperature derivative of the bulk modulus is close within its uncertainty though (Table 3). The behavior of negative thermal expansion for the  $c$ -axis (Fan et al. 2015) in beryl but not in this tourmaline sample can be an explanation for its smaller thermal expansion coefficient. Similar to the compression anisotropy of the  $a$ -axis and  $c$ -axis for this tourmaline sample, the thermal expansion of these two axial directions are also anisotropic with that the value of  $\alpha_{c0}$  is about 2.40 times larger than that of  $\alpha_{a0}$  (Table 4). Against the anisotropic property of compression, the  $c$ -axis has a smaller isothermal bulk modulus but get a larger thermal expansion and the  $a$ -axis is less expansive. Interestingly, in this study of tourmaline the degrees of anisotropy for compression and thermal expansion ( $K_{a0}/K_{c0}$  and  $\alpha_{c0}/\alpha_{a0}$ ) are very close (Table 4).

**Table 3** Thermal expansion coefficients and temperature derivatives of the bulk moduli of tourmaline and beryl

Sample	$(\partial K/\partial T)_P$ (GPa K <sup>-1</sup> )	$\alpha_0$ (10 <sup>-5</sup> K <sup>-1</sup> )	Method	References
Elbaite		1.68 <sup>a</sup>	Strain gauge	Tatli and Pavlovic (1988)
Schorl		1.55 <sup>a</sup>		
Uvite		1.47 <sup>a</sup>		
Elbaite–schorl		1.77 <sup>a</sup>	Dilatometry	Pandey and Schreuer (2012)
Elbaite–schorl		1.69 <sup>a</sup>		
Elbaite–schorl		1.62 <sup>a</sup>		
Schorl–dravite		1.46 <sup>a</sup>		
Schorl–dravite		1.48 <sup>a</sup>		
Elbaite		4.56	Powder XRD	Donnay (1977)
Uvite	-0.009 (6)	4.39 (27)	Powder XRD	This study
Beryl	-0.017 (4)	0.282 (74)	Powder XRD	Fan et al. (2015)

XRD X-ray diffraction

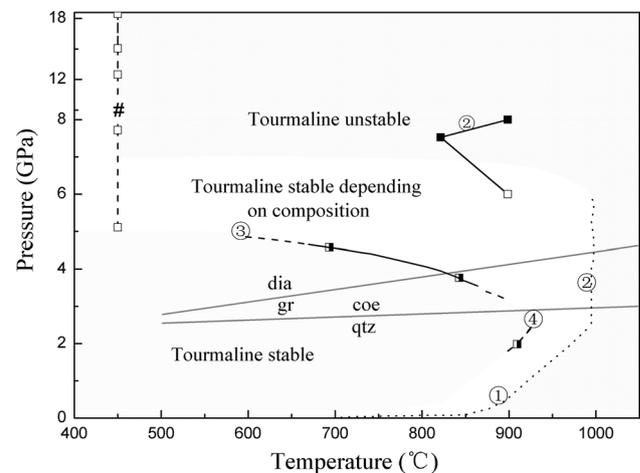
<sup>a</sup> Calculated from the linear expansion coefficients  $\alpha_{a0}$  and  $\alpha_{c0}$ **Table 4** Linear axial thermoelastic parameters of the tourmaline sample in this study

$K_{a0}$ (GPa)	$K'_{a0}$	$K_{c0}$ (GPa)	$K'_{c0}$	$\alpha_{a0}$ (10 <sup>-5</sup> K <sup>-1</sup> )	$\alpha_{c0}$ (10 <sup>-5</sup> K <sup>-1</sup> )	$K_{a0}/K_{c0}$	$\alpha_{c0}/\alpha_{a0}$
138 (2)	11.8 (6)	60 (1)	10.9 (5)			2.288 (9)	+
139 (2)	11.5 (7)	59 (1)	11.4 (5)	1.00 (11)	2.41 (24)	2.339 (4)	2.396 (31) *

+ Calculated from  $P$ - $V$  data at 300 K; \* calculated from all  $P$ - $V$ - $T$  data

## Geochemical and geophysical implications

In previous studies, tourmaline has been proved to be stable at ultrahigh-pressure conditions based on petrologic and experimental investigations (e.g., Krosse 1995; Werding and Schreyer 1996; Von Goerne et al. 1999; Kawakami 2001; Ota et al. 2008a; Dutrow and Henry 2011). In addition, the localized B isotope anomalies adjacent to convergent margins are possibly caused by tourmaline which carries B isotopes of sediments into deep mantle (Nakano and Nakamura 2001). For a single-phase, dravite  $[\text{NaMg}_3\text{Al}_6(\text{BO}_3)_3\text{Si}_6\text{O}_{18}(\text{OH})_4]$  has been proved to be decomposed at temperatures larger than 1000 °C at 3–5 GPa, and 6–8 GPa at 900 °C (Krosse 1995; Werding and Schreyer 1996), which suggest that tourmaline is stable from Earth's surface to the depth of subarc. Recently, Ota et al. (2008a) investigated the stability of tourmaline  $[(\text{Na}_{0.79}\text{Ca}_{0.03}(\text{Mg}_{1.97}\text{Fe}_{0.58}\text{Al}_{0.21})\text{Al}_6(\text{BO}_3)_3\text{Si}_{6.05}\text{O}_{18}(\text{OH})_4)]$  in a metapelitic system under high pressure and high temperature and observed that tourmaline breaks down at pressures of 4.5–5 GPa at 700 °C and 4–4.5 GPa at 800 °C, thus concluding that tourmaline breaks down before reaching the depth of 150 km. In this study, however, stability of a uvite-dominated sample was studied at pressures up to ~18 GPa and temperatures up to 450 °C, which implied that tourmaline may be stable under higher pressures than that of previous studies (Krosse 1995; Werding and Schreyer 1996) at relatively low temperatures (Fig. 8). This study suggests that tourmaline could be stable in a greater depth of



**Fig. 8**  $P$ - $T$  stability estimates for tourmaline of various compositions based on constrained from natural samples (circle) and experimental data (squares), with extrapolations (dashed lines). Selected reaction boundaries (gray lines) are shown for reference. Dravite: (1) Robbins and Yoder (1962); (2) Krosse (1995); (3) Ota et al. (2008a, b). Magnesio-foitite: (4) Werding and Schreyer (1996). Uvite: (#) This study. (Note that this picture is drawn according to “Fig. 3” from Dutrow and Henry 2011). *dia* diamond, *gr* graphite, *coe* coesite, *qtz* quartz

Earth's interior than previous estimates in relatively cold conditions such as subduction zones. Actually, such conditions may exist in old and rapidly subducting slabs, for example, in northern Tonga where cold slab temperatures (about 700 K) could be preserved to a great depth

(~540 km) based on its subduction zone thermal model (Bina and Navrotsky 2000). However, no evidence that uvite and other tourmaline occur in subducted lithospheres so far, and temperatures at the surfaces of slabs are generally larger than that of interiors (e.g., Kincaid and Sacks 1997; Poli and Schmidt 2002), both are not beneficial for transporting tourmaline into deep Earth along with subducting slabs. Consequently, this study of the  $P$ – $T$  stability of natural uvite-dominated tourmaline sample cannot be a direct proof that uvite or other tourmaline minerals can be transported into deep Earth (e.g., mantle) along with subducting slabs. Nonetheless, uvite-dominated tourmaline is stable in such a high pressures (up to 18 GPa) at relatively low temperatures (450 °C), which implies that tourmaline can possibly survive in deep-Earth conditions which occur in old and rapidly subducting slabs (like Tonga).

## Conclusions

Using a modified Merrill–Bassett-type DAC coupled with synchrotron X-ray diffraction, we carried out the phase stability and  $P$ – $V$ – $T$  measurements on a natural tourmaline sample with the composition of uvite domination, at pressures between 0 and 18 GPa and temperatures up to 723 K. The thermoelastic properties of this sample have been derived by fitting the  $P$ – $V$ – $T$  data using high-temperature BM EoS and then obtained the zero-pressure volume, isothermal bulk modulus and its pressure derivative, thermal expansion coefficient and the temperature derivative of the bulk modulus. The axial moduli and thermal expansivities were also obtained by fitting a “linearized” BM EoS, which showed the anisotropic compression [ $K_{a0} = 139$  (2) GPa and  $K_{c0} = 59$  (1) GPa] and thermal expansion [ $\alpha_{a0} = 1.00$  (11)  $\times 10^{-5}$  K $^{-1}$  and  $\alpha_{c0} = 2.41$  (24)  $\times 10^{-5}$  K $^{-1}$ ].

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